

Signaling motives in lying games

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Abstract

This paper studies the implications of agents signaling their moral type in a lying game. In the theoretical analysis, a signaling motive emerges where agents dislike being suspected of lying and where some lies are more stigmatized than others. The equilibrium prediction of the model can explain experimental data from previous studies, in particular on partial lying, where individuals lie to gain a non payoff-maximizing amount. I discuss the relationship with theoretical models of lying that conceptualize the image concern as an aversion to being suspected of lying and provide applications to narratives, learning, and the disclosure of lies.

Keywords: honesty, image concerns, lying, psychological game theory

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1 Introduction

The virtue ethics of the ancient Greeks recognize honesty among the desirable moral characteristics which can lead individuals to flourish and to live a “good life”.¹ Religious texts and popular myths often stress the value of honesty.² Honesty also plays a role in economic situations; if Alice is a buyer and Bob is a seller in a credence goods market, it will be relevant for Alice not just to ask if Bob was honest with her in the exchange they just had, but whether Bob will be honest again in future exchanges. To form this latter expectation, Alice needs to have an idea about Bob’s moral character, in particular about his honesty. This paper is concerned with the strategic implications when individuals want to appear honest.

In strategic situations where different agents have different objectives and where some agents are better informed than others, truthful communication can be difficult or impossible. This impedes information transmission and can lead to market failures (Akerlof, 1970, Crawford and Sobel, 1982). Some of these inefficiencies can be overcome if lying is costly for agents (Kartik, 2009), but the size and form of lying costs is mainly an empirical question.

More recently, a literature has emerged that empirically investigates lying costs in laboratory experiments. In an experiment, Fischbacher and Föllmi-Heusi (2013)—or F&FH—gave participants a six-sided die. Participants were instructed to roll the die in private and report the number they rolled to the experimenter. Upon reporting, participants received a payoff in Swiss Franks that corresponded to their die roll, except for number six, which paid nothing. Since the objective distribution of the die roll is known, lying behavior can be inferred from the aggregate report distribution. F&FH find that the empirical distribution of reports is consistent with some participants reporting honestly and other participants lying. In various follow-up experiments—that sometimes let participants flip coins instead of rolling a die—similar patterns emerge (Abeler, Nosenzo, and Raymond, 2019).

One robust feature in experiments that use the F&FH die-roll task is that some in-

¹See e.g. the Stanford Encyclopedia article on Virtue Ethics (Hursthouse and Pettigrove, 2018).

²Consider for example the cherry tree myth about a young George Washington who cuts down his father’s tree with a hatchet. After finding the cut-down tree, the father confronts his son. Young George confesses and the father promptly embraces him because “*Such an act of heroism in my son is more worth than a thousand trees*” (Weems, 1918). The implied moral seems clear—George Washington did not only become a historical figure but did so honestly. His example should serve to inspire others to also be honest.

dividuals lie and dishonestly report four when they could have earned more money by lying and reporting five. One reason for the observed behavior could be that individuals dislike being suspected of lying; since fewer individuals lie to report a number that does not maximize their monetary payoff, reporting a lower number evokes less suspicion. Papers by [Dufwenberg and Dufwenberg \(2018\)](#), [Gneezy, Kajackaite, and Sobel \(2018\)](#) and [Khalmetzki and Sliwka \(2019\)](#) provide theoretical models that formalize this intuition.³ In doing so, they all have to come to terms with the fact that lying decisions depend on perceived suspicion, which in turn depends on lying decisions. Suspicion therefore is an equilibrium outcome of a game between an agent and an observer, in which an agent draws a state (a number on a die, a coin flip) and makes a report to an observer. The report serves as a signal to the observer, who in turn forms a belief about the likelihood that the agent lied; a measure of suspicion. Anticipating this, the agent will take their belief over the observer's belief into account when deciding what to report. The agent's utility is *belief-dependent*, as it depends on the perceived *image* that the observer attaches to the agent after hearing the report. In their meta-study, [Abeler et al. \(2019\)](#)—from now on [AN&R](#)—conclude that such image concerns are key to explain the stylized empirical facts observed in experiments on lying.

While image concerns are deemed to be important, there are different ways to conceptualize them. [AN&R](#) find that two kinds of image concerns can explain the observed empirical regularities in lying games. The first is an image concern that (in various forms) is used in models by [D&D](#), [GK&S](#), and [K&S](#), where individuals want to signal that they did not lie.⁴ The second is a lying model where the signaling motive is similar to the honor-stigma model of [Bénabou and Tirole \(2006\)](#)—hereafter [B&T](#). In this model, individuals want to appear as someone who is intrinsically honest. The main difference between both approaches is that in the former individuals want to signal a good deed (they did not lie), whereas in the latter model individuals want to signal a moral character (they are intrinsically honest). In this paper, I ask if this second approach to image concerns can provide useful insights and extend our understanding of lying behavior. I derive a lying model based on [B&T](#), which so far has only received

³From now on in the text I will refer to them as [D&D](#), [GK&S](#), and [K&S](#) respectively.

⁴[GK&S](#) and [K&S](#) introduce the image concern as either the probability to have told the truth, conditional on the report, or as the probability to have lied, conditional on the report. [D&D](#) further interact the conditional probability to have lied with the perceived size of the lie. For example, in [D&D](#) the agent gets a lower image if they are suspected of reporting a five instead of a one than if they are suspected of reporting a four instead of a three.

cursory attention in the literature.⁵

I study the strategic implications of individuals signaling their moral character in a lying game. Agents draw a random number (by rolling a die, flipping a coin, etc.) and make a report to an observer. They are morally concerned and incur a cost if their report does not equal their draw. Agents differ in the extent to which they are morally concerned; some suffer high and others low costs from lying. Individual types are private, but in equilibrium the agents' reports are informative about their type. This happens because worse moral types are more likely to dishonestly report a high number than better types. In the model, *credibility* of the report and the *composition* of types reporting it influences an agent's social image. A report is more *credible* the more likely it is that it was made truthfully. Moreover, the reputation attached to a report depends on the moral type of the liars reporting it.

To illustrate how reputations form in the character-based model, consider the following example of a professor who, on the day of a final exam, receives messages from some of her students that they are sick and cannot participate in the exam. By university guidelines, sickness is the only acceptable excuse for not writing the exam. Students also find it sufficiently unpleasant to write an exam when they are sick, so that every sick student will send a message to the professor. There might, however, also be reasons that induce a healthy student to send a message that they are sick. Suppose that some of the students who are not sick are in an *emergency*. Students who are neither sick nor in an emergency and excuse themselves from the exam are *shirking*. Professing to be sick when one is not constitutes a lie. Students dislike lying to different degrees, with some students being more moral (having a higher lying cost) than others. A healthy student will lie and claim to be sick if the benefits from not writing the exam are higher than their lying cost. Since writing the exam is arguably worse when in an emergency, more students will lie with than without an emergency. We can observe that this type of behavior implies sorting of moral types into falsely claiming sickness or not. Those in the left tail of the moral type distribution will lie about their health status while those in the right tail of the distribution will not. The threshold that divides the moral type

⁵Proposition 7 in AN&R, appendix B, provides some general properties of such a model. Their analysis however remains too general to complement the insights derived from the deed-based image model. Indeed, the result that concludes AN&R's meta-study (Finding 10) cannot distinguish between a model that employs a deed-based image concern and a model that uses a character-based image concern as both account for exactly the same empirical facts ("*Only the Reputation for Honesty + LC [deed-based image] and the LC-Reputation [character-based image] models cannot be falsified by our data*" (AN&R, p. 1144)).

distribution into a left and a right tail depends on the reasons that students have to lie about their health status. It will be higher for students with than without an emergency, which implies that, for students with an emergency, the left tail is comparatively larger and the right tail is smaller. Figure 1 sketches out the sorting process from possible states of the worlds into student actions.

Figure 1. Sorting from states of the world into actions



The professor does not observe the real reason of a student who claims to be sick. Therefore, upon receiving a message from a student, the professor forms a posterior expectation about the student’s expected moral character by weighing all different potential motives behind sending the message with their empirical frequency. The posterior expectation after receiving a message will always be lower than the professor’s prior expectation about the student, before receiving the message. This is because the professor cannot distinguish between truthful and dishonest messages—while actual sickness is not correlated with moral types, the students who send a dishonest message pool with students who send a truthful message, and those who send the dishonest message come from the left tail of the type distribution, i.e., they are of a low expected moral type. In line with the idea that individuals want to be perceived of high moral character, a student’s reputation is equal to (her beliefs about) the professor’s posterior expectation. Now suppose that there is a (potentially pandemic-induced) increase in the probability that a student is sick at the exam date. All things equal, such an increase will increase the professor’s posterior expectation. This reflects the credibility effect—if more students are actually sick, it is more likely that any student claiming to be so is telling the truth. Alternatively, consider an increase in the probability that any student faces an emergency at the exam date (which might also be pandemic-induced as they have to care for sick family members). Such an increase will also increase the professor’s posterior expectation, as, conditional on not being sick, it is less likely that the student is simply shirking. This reflects the composition effect—even though they may still lie,

students in an emergency who claim to be sick on average are of a higher moral type than students who shirk.

In the die roll game, the character-based model predicts an equilibrium that can include partial lying. Recall that agents have a financial incentive to overstate their number. Therefore, if some agents lie to report the highest paying number, this number will on average be reported by worse moral types. Because agents are image concerned, they might then have an incentive to leave some money on the table in exchange for a higher image by reporting the second highest or even lower payoff when they lie. This dynamic generates an equilibrium with characteristics that are similar to the deed-based image models of [GK&S](#) and [K&S](#); agents lie only if they draw a number that is smaller than or equal to some threshold and report a number that is above the threshold. Under an equilibrium refinement that restricts liars to play symmetric strategies, this is the unique outcome of the game.

I apply the model to study the role of beliefs that agents hold about others and the disclosure of lies. A reoccurring theme will be that the effects of most interventions will depend on the interplay between credibility and composition effects. The credibility effect leads to the kind of disguised behavior that much of the literature has focused on. It always leads to strategic substitutability of actions, as agents are motivated to not raise suspicion, therefore wanting to lie when unsuspected and wanting to tell the truth otherwise. Through the composition effect, situations with strategic complementarities can be created where agents lie because “everyone is doing it” or where they may be excessively honest because lying just “is not done”. The character-based model thus provides a parsimonious framework for the disguised behavior that deed-based models focus on and the social norm aspect of the honor-stigma model.

The following section presents the model. Parts [2.1](#) and [2.2](#) discuss the setup and equilibrium properties. I apply the model to investigate the determinants of reputation in [Section 3](#). [Section 4](#) applies previous insights to investigate the behavioral effects of interventions that change agents’ beliefs and detect liars. Throughout this section, I contrast predictions of the character-based model with predictions from a deed-based model. I provide extensions of the model in [Section 5](#). [Section 6](#) discusses related theoretical and experimental literature. The paper concludes in [Section 7](#). Proofs of all formal results appear in [Appendix A](#).

2 Model

2.1 Setup

Game form Consider a game between a continuum of agents and an observer. Each agent draws a state $j \in \{1, \dots, K\}$, which is randomly determined by nature. The agents can be thought to be participants in an economic experiment who are asked by the experimenter, who is the observer, to roll a die. In this case, the state would be the outcome of a die roll. An alternative interpretation of the setup could see agents as students who, at the day of an exam, are either sick or healthy and either are in an emergency or not. Throughout this section, we will focus on the first interpretation. In line with the die roll analogy, we make the simplifying assumption that the state is distributed uniformly on its domain.

After the draw, agents each make a report $a \in \mathcal{K} = \{1, \dots, K\}$ to the observer and receive a total payoff consisting of direct and image payoffs, as described below. The observer is a passive player with no action whose payoff we do not further specify.

Direct payoffs Agents know their state j and make a report a , which earns them a direct payoff $y(a)$, where $\Delta(a, a - 1) \equiv y(a) - y(a - 1) > 0$. The payoff scheme might reflect the experimenter’s choice of rewards for reporting certain numbers of the die. Alternatively, the agent-as-student would always earn the highest payoff by claiming to be sick and excusing themselves from the exam.

Reporting $a \neq j$, agents incur cost t which is heterogenous across agents. This cost arises through a purely intrinsic, moral preference for honesty. That individuals are heterogeneous in their preferences for honesty is documented in experiments such as [Gibson, Tanner, and Wagner \(2013\)](#), [Gneezy, Rockenbach, and Serra-Garcia \(2013\)](#), and [Kajackaite and Gneezy \(2017\)](#). [Gibson et al. \(2013\)](#) in particular show that the lying cost distribution function consists of many intermediate types, who begin to lie if the returns to lying are high enough. The intrinsic preference for honesty reflects that agents feel bad for lying. Modeling lying costs as fixed seems appropriate as a first approximation based on the evidence from observed lying games reported by [AN&R](#) and [GK&S](#), where the experimenter sees individual draws and reports. The data from these experiments shows a “missing middle” pattern, where individuals either tell the truth or lie to report the highest number, with only a minority of liars reporting a number in between. This suggests that cost functions that increase in the size of the

lie, and which therefore could rationalize partial lying for intrinsic reasons, do not accurately describe lying behavior in these experiments. I discuss more complex cost functions where the size of the lie is interacted with the moral type as an extension in Section 5. The lying cost is unknown to the observer, who however knows that it is drawn from a distribution $F(t)$ with full support on $(0, \bar{t}]$ and which is independent of j . \bar{t} is a large number, to be specified in detail below.

I will use “lying cost” and “moral type” interchangeably when discussing t , as this section considers honesty as the only relevant moral dimension. This is due to the setup of the game, which reflects laboratory lying games and elements of verbal communication. In these settings, lying comes at no expense to a third party, which allows us to exclusively focus on honesty.⁶ Further morality dimensions, such as altruism, might become relevant and interact with honesty in settings where agents cheat someone else, for example, stealing (footnote 18 in section 3 provides further discussion of this point).

Image payoffs In addition to being intrinsically honest, agents also value a reputation for honesty. There can be instrumental reasons to value such a reputation. An expert might prefer to appear honest to build an enduring relationship with an advisee. A student who hopes to receive a good letter of support from their professor wants to appear sincere to them. There are also noninstrumental reasons for why an agent might prefer to look honest; many individuals want to appear moral and one indicator of morality is honesty. This type of image concern follows B&T and other approaches in psychological game theory that formalize the idea that individuals want to signal “good traits” (Battigalli and Dufwenberg, 2022): Through their actions, agents tell others something about their intrinsic preferences, and agents want to look as if they have preferences which are valued by an observer. To make an inference, the observer forms a belief about the expected moral type of an agent reporting a , denoted as $\mathcal{R}_a = \mathbb{E}(t|a)$. The image payoff equals the reputation weighted by a scalar $\mu > 0$,

$$\mu \mathcal{R}_a,$$

where μ is not too large, so that agents are not disproportionately sensitive to changes in the image payoff.⁷

⁶The setup might further reflect tax reporting, where individual contributions are a negligible part of total tax earnings.

⁷If μ is large multiple equilibria can obtain. An explicit upper bound will depend on the preference

Utility Direct and image payoffs add up to total payoffs, or utility. An agent of type (j, t) who reports a earns utility

$$u(j, t, a) = y(a) - 1_{a \neq j}t + \mu \mathcal{R}_a.$$

I now assume that the maximum lying cost is a number $\bar{t} > \Delta(K, 1) + \mu \mathbb{E}(t)$. The assumption ensures, in line with the empirical evidence provided by [AN&R](#), that there are agents who never lie, regardless of the state they draw. One immediate consequence of the assumption is that the observer always puts a positive probability on any state being reported. This property is helpful when solving for the equilibrium, as described next.

2.2 Equilibrium

The structure of the game makes it a *psychological game* ([Geanakoplos, Pearce, and Stacchetti, 1989](#), [Battigalli and Dufwenberg, 2009](#)), as the final payoffs of agents depend on the observer's beliefs about the agents' moral type. Agents' strategies s map their type into a distribution over reports. Denote the probability of an agent of type (j, t) reporting a by $s(a|j, t)$. In the following, an agent is a *liar* if they choose a *dishonest* strategy where $s(a = j|j, t) = 0$. To put it another way, an agent who never tells the truth is a liar. Conversely, a *truth-telling* agent is an agent with a strategy $s(a = j|j, t) = 1$.

The following equilibrium definition invokes the standard conditions of utility maximization and that agents and the observer correctly apply Bayes' rule and have a common prior. This definition follows the literature and serves as a useful yardstick to think through strategic interdependencies. Since the maximum lying cost is high, every state is reported with positive probability in equilibrium. This implies that Bayes' rule can be applied to calculate the equilibrium reputation of every state, obliterating the need for further equilibrium refinements to pin down beliefs that are off the equilibrium path.

Definition 1. *An equilibrium is defined by strategies $s(a|j, t)$, where*

- $s(a = j|j, t) \geq 0$, $s(a \neq j|j, t) \geq 0$ and $\sum_{k \in \mathcal{K}} s(a = k|j, t) = 1$ for all j and t .
- $s(a|j, t) > 0$ if and only if $a \in \arg \max_{a \in \mathcal{K}} y(a) - 1_{a \neq j}t + \mu \mathbb{E}(t|a)$.

distribution function. The Appendix shows that $\mu \leq 1$ is sufficient if $F(t)$ is log-concave.

- *Agents and the observer hold the correct equilibrium beliefs*

$$\mathcal{R}_j = \frac{\sum_{l \in \mathcal{K}} \int_0^{\bar{t}} s(j|l, t) t f(t) dt}{\sum_{l \in \mathcal{K}} \int_0^{\bar{t}} s(j|l, t) f(t) dt} \text{ for } j \in \mathcal{K}.$$

2.2.1 General results

Based on the definition, we can derive general properties that hold in any equilibrium of the game. Since they should be familiar to readers familiar with the literature, I relegate a formal discussion of them to the Appendix and give intuitions below.

Proposition 1. *In an equilibrium*

- (i) *If $s(a = k|j, t) > 0$ and $s(a = l|j, t) > 0$ for some type (j, t) with $j \neq k$ and $j \neq l$, then $y(k) + \mu \mathcal{R}_k = y(l) + \mu \mathcal{R}_l$.*
- (ii) *If there is a type (j, t) with $j \neq k$ for which $s(a = k|j, t) > 0$, then $s(a = k|k, t) = 1$ for all types (k, t) and $s(a = j|l, t) = 0$ for all types (l, t) with $l \neq j$.*
- (iii) *There is a type (j, t) with $j < K$ for which $s(a = K|j, t) > 0$ and for all types (j, t) with $j > 1$, $s(a = 1|j, t) = 0$.*
- (iv) *If $K > 2$ and the ratio $\Delta(K, K - 1)/\mu$ is sufficiently small, then there is a type who will lie and report a number different than K .*

Point (i) says that, when ignoring type-dependent lying costs, every state that is dishonestly reported by some liars yields the same payoff. It can be seen by arguing by contradiction; if there were a state that paid a higher material plus reputational payoff than any other state, then agents would only dishonestly report that state. Point (ii) follows by a similar logic, stating that if someone lies to report k , then no agent lies after drawing k and that if someone lies after drawing j then no agent lies to report j . These results are driven by the assumptions that lying costs are fixed and that the image payoff weight μ is the same for every agent. Both assumptions taken together imply that liars have the same preferences over reporting any state after incurring the type-dependent lying cost. If multiple states are reported dishonestly, liars have to be indifferent between reporting any of them. Section 5 discusses how results change under heterogenous image concerns.⁸

⁸Homogenous image concerns are commonly assumed in the literature. They offer tractability. In

Point (iii) seems natural but contains a somewhat deeper point that is worth highlighting. Low moral types are more likely to lie than high moral types. Because of this, reporting a state that is reported by liars in equilibrium decreases the observer’s prior belief in expectation. Reporting other states conversely increases the observer’s prior. Suppose an equilibrium exists where no liar reports state K . Then, the observer would have to increase her prior expectation after hearing a report of K . Liars in such an equilibrium would always prefer to report K over any other state to gain the highest possible direct payoff and to simultaneously increase the observer’s prior expectation. This contradicts utility maximization. A symmetric argument can be made to show that no liar will ever report 1.

The last point (iv) follows because, with image concerns, liars trade off direct payoffs with image payoffs. The image payoffs of states gets spoiled by the liars reporting it. It is therefore beneficial for liars to report more than one state to “smooth out” the image losses they create over multiple states.

2.2.2 Equilibrium refinement, main prediction

The predictions above can be useful, but they are also relatively unspecific. One reason is that the equilibrium definition allows for a very rich variety of strategies that liars can play, some of which that might appear “strange”, or, at least, would require a considerable amount of coordination among liars. For example, with $K = 4$, there can be an equilibrium in which some liars from 1 lie up to report 2 and some agents from state 3 lie down and also report 2. This equilibrium can be sustained if liars coordinate on their moral type; that is, the liars with the highest intrinsic type report 2 while those with the lowest intrinsic type report 4. Such behavior can be seen as problematic. Because lying costs are fixed, liars, conditional on lying, have the same preference ranking among reports. There is no a priori reason why a liar would report one state over another if they are indifferent over both. The degree to which liars have to coordinate to support such an equilibrium motivates a refinement that restricts agents to symmetric lying strategies, as defined below.⁹

an experiment, [Friedrichsen and Engelmann \(2018\)](#) provide evidence for heterogenous image concerns, though less is known about whether participants take into account heterogenous image concerns in others.

⁹Appendix B gives an example of an asymmetric equilibrium where liars condition their strategies on their moral type.

Definition 2. *Agents play symmetric lying strategies if $s(a = k|j, t), s(a = k|j', t') > 0 \Rightarrow s(a = k|j, t) = s(a = k|j', t')$ for any $t, t' \in (0, \bar{t}]$, $j, j' \in \mathcal{K} \setminus \{k\}$.*

Lying strategies are symmetric when the agents' type (j, t) determines whether they lie or not, but does not determine which state they report. Similar properties are imposed by [D&D](#) (“uniform cheating”) to obtain their main result and by [K&S](#) to generate comparative statics predictions. Symmetric lying strategies imply that liars randomize in the same way which state to report dishonestly. While there are few direct tests of mixed lying strategies, evidence from [F&FH](#) is seemingly in line with this refinement. They show that the reports of participants who participate in a die-roll experiment for a second time, and who reported the highest payoff in the first experiment, are indistinguishable from the second-time reports of participants who reported the second-highest payoff in the first experiment. If liars had further conditioned their reports on some intrinsic attributes, we would expect the reports of those who report the highest state to be systematically different from those who report the second highest state.¹⁰

Solving the model under symmetric strategies gives the main result.

Proposition 2. *There exists a unique equilibrium when agents play symmetric lying strategies. It has the following properties:*

- (i) *The report distribution is strictly increasing in j .*
- (ii) *\mathcal{R}_j is strictly decreasing in j .*
- (iii) *No agent who draws j reports a state $k < j$.*
- (iv) *$s(a \neq j|j, t) > 0$ only if $j \leq k^*$, where $k^* \in \mathcal{K} \setminus \{K\}$.*

The equilibrium of the game is of the following type: Agents lie only if they draw a state smaller or equal than some threshold state k^* . If they lie, they report a state larger than k^* . State K is reported by most agents, followed by $K - 1$, and so on. In what follows, I discuss the equilibrium properties and provide a sketch of the proof. I relegate the technical details to [Appendix A](#).

Equilibrium properties I will refer to states that are reported by liars as *high states* and states that are not reported by liars as *low states*. The set of high states is \mathcal{H} . Agents will

¹⁰[F&FH](#) also show that participants who make reports lower than the second-highest payoff in the first experiment are more likely than others to make reports lower than the second-highest payoff in the second experiment, implying that decisions are to some extent consistent across both experiments.

either report the state that they drew or one of the high states. Since liars are indifferent between reporting any of the high states in equilibrium, the decision problem becomes binary: agents will prefer lying over telling the truth if and only if they prefer reporting K over the state that they drew. Conditional on lying, they will randomize over reporting any of the high states. Therefore, an agent of type (j, t) will lie if and only if $t \leq \hat{t}_j$ for a cutoff \hat{t}_j that, if interior, solves

$$y(K) - \hat{t}_j + \mu\mathcal{R}_K = y(j) + \mu\mathcal{R}_j.^{11}$$

Truth-tellers therefore comprise the upper tail of the preference distribution and liars make up the lower tail. Truth-tellers and liars who draw a state j have an expected moral type of respectively

$$\begin{aligned}\mathcal{M}^+(\hat{t}_j) &\equiv \mathbb{E}(t|t > \hat{t}_j) \geq \mathbb{E}(t), \\ \mathcal{M}^-(\hat{t}_j) &\equiv \mathbb{E}(t|t \leq \hat{t}_j) < \mathbb{E}(t).\end{aligned}$$

The first term is larger than the second, which reflects that liars are stigmatized while truth-tellers are honored. It follows that the reputation of a low state j is equal to $\mathcal{M}^+(\hat{t}_j)$ and a fraction $F(\hat{t}_j)$ of agents who draw that state are liars. We collect all cutoffs \hat{t}_j of each state in a vector $\hat{\mathbf{t}}$ and define the *expected moral type of liars* by

$$\mathcal{L}(\hat{\mathbf{t}}) \equiv \sum_{j \in \mathcal{K}} \text{P}(\text{draw } j|\text{lie}) \mathcal{M}^-(\hat{t}_j), \text{ with } \text{P}(\text{draw } j|\text{lie}) = \frac{F(\hat{t}_j)}{\sum_{k \in \mathcal{K}} F(\hat{t}_k)}. \quad (1)$$

The probability of a liar reporting j (conditional on lying) is α_j , with corresponding vector $\boldsymbol{\alpha}$. Any high state is reported honestly by a fraction $1/K$ of all agents and by a fraction of $1/K \times \alpha_j \sum_{j \in \mathcal{K}} F(\hat{t}_j)$ liars. The probability that a randomly chosen agent reporting j is telling the truth is

$$r_j \equiv \text{P}(\text{truth}|\text{report } j) = \frac{1}{1 + \alpha_j \sum_{j \in \mathcal{K}} F(\hat{t}_j)}.$$

The reputation of any high state becomes a weighted average between the expected

¹¹The assumption that $\bar{t} > \Delta(K, 1) + \mu\mathbb{E}(t)$ ensures that the l.h.s. will be smaller than the r.h.s. for some $t < \bar{t}$. If the l.h.s. is weakly smaller than the r.h.s. for $t = 0$, no agent is going to lie after drawing j . These are the high states in which $\hat{t}_j = 0$.

type of truth-tellers (which equals the prior) and the expected type of liars;

$$\mathcal{R}_j = r_j \mathbb{E}(t) + (1 - r_j) \mathcal{L}(\hat{t}) \text{ if } j \in \mathcal{H}. \quad (2)$$

The above expression is smaller than the observer's prior expectation $\mathbb{E}(t)$ as it is a convex combination of $\mathbb{E}(t)$ and $\mathcal{L}(\hat{t})$. We have seen before that the reputation of low states is higher than the prior expectation. One immediate consequence is that there is no downwards lying in equilibrium (part (iii) of Proposition 2): Reporting a state that pays less than the initial draw would imply a lower image payoff and a lower direct payoff, which is inconsistent with utility maximization.¹² Part (iv) of the proposition is a direct implication of part (iii).

Turning to part (ii) in the proposition, decreasing reputations, it is useful to distinguish between low states and high states. Among the low states, reputations decrease as the direct payoff of a state increases because, as the direct payoff increases, agents have a smaller direct incentive to lie. For example, agents who report 1, despite having a high incentive to lie, send a higher signal about their intrinsic honesty than agents who report k^* . Reputations also intuitively decrease among high states because liars trade off direct payoffs for image payoffs. As the direct payoff of a high state decreases, its reputation has to increase to insure that liars are indifferent among high states.

Decreasing reputations imply increasing reporting frequencies; among low states, there is an inverse relation between the reputation of the state and the proportion of agents who report it. With symmetric lying strategies, the same relation holds among high states, as the reputation of any state is decreasing in the proportion of liars that are reporting it. Therefore, in the proposition, (i) is a consequence of (ii).

Existence Constructing the equilibrium is seemingly complicated because it involves a threshold state k^* , a vector of cutoff types \hat{t} , and a vector of probabilities $\mathbf{r} = (r_1, \dots, r_K)$ that each depend on one another. The key step in the proof is to realize that we can fix the reputation of state K , which is always reported dishonestly in equilibrium, at some level φ . We can then define a function which implicitly defines threshold types as a function of φ ;

$$\mathcal{T}(t, \varphi, \Delta(K, j)) \equiv \Delta(K, j) + \mu[\varphi - \mathcal{M}^+(t)] - t = 0.$$

Since this equation is strictly decreasing in t there is always a unique solution for a given

¹²Note the role of the symmetry refinement here. Many of the counterintuitive equilibria without symmetry emerge because without symmetry $\mathcal{R}_j > \mathbb{E}(t)$ is possible for some (but not all) states $j \in \mathcal{H}$.

φ , which we denote as $\tilde{t}_j(\varphi)$. The threshold type of state j is $\hat{t}_j(\varphi) = \max \{\tilde{t}_j(\varphi), 0\}$.

Aggregating thresholds in a function

$$S(\varphi) \equiv \frac{1}{K} \sum_{j \in \mathcal{K}} F(\hat{t}_j(\varphi))$$

gives the fraction of agents that are willing to lie if the reputation of state K is φ . This function can be thought of as characterizing the supply of lies.

Plugging the threshold functions into (1), the expected moral type of liars indirectly depends on φ through \mathbf{t} ;

$$\mathcal{L}(\hat{\mathbf{t}}(\varphi)) = \sum_{j \in \mathcal{K}} \frac{F(\hat{t}_j(\varphi))}{\sum_{k \in \mathcal{K}} F(\hat{t}_k(\varphi))} \mathcal{M}^-(\hat{t}_j(\varphi)).$$

We can then observe that the equilibrium reputation of state K , φ^* , must be between $\mathcal{L}(\mathbf{t}(\varphi^*))$ and $\mathbb{E}(\mathbf{t})$, as the reputation is a weighted average of the expected moral type of the liars and truth-tellers reporting it. We can use the expected moral type of liars and Equation (2) to write r_K as a function of φ . Liars are indifferent between all high states, which allows us to derive a function $r_j(\varphi)$ for all remaining states $j \in \mathcal{H}$.

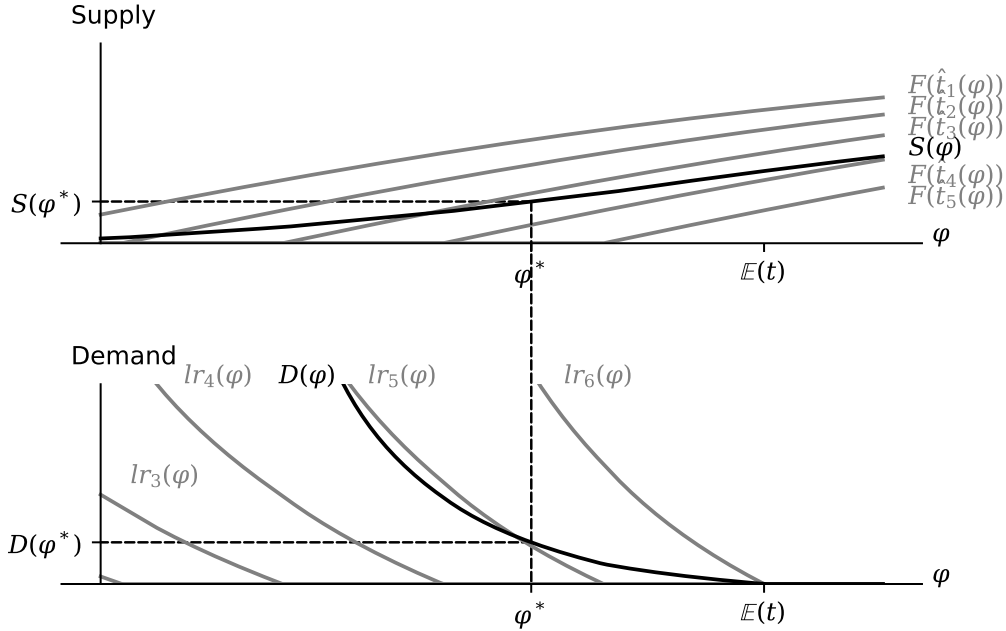
Transforming $r_j(\varphi)$ to a likelihood ratio $lr_j(\varphi) \equiv \frac{1-r_j(\varphi)}{r_j(\varphi)}$ gives the ratio of liars to non-liars reporting j if the reputation of the highest state is φ . Adding up the likelihood ratios and normalizing by $1/K$, we arrive at a function

$$D(\varphi) \equiv \frac{1}{K} \sum_{j \in \mathcal{H}} lr_j(\varphi).$$

This function returns the proportion of agents who lie as a function of φ . It can be interpreted as a demand function, as it gives the fraction of liars that are needed to sustain an equilibrium for a given reputation of the highest state.

Figure 2 illustrates the functions S and D . The upper panel shows the individual threshold functions and the aggregate supply function. An increase in the reputation of state K makes it more attractive for agents to lie, which is why the function slopes upwards. The lower panel shows the demand side. These functions slope downwards. Intuitively, when φ is low, many liars will report states different from K to alleviate

Figure 2. Equilibrium



reputational losses. However, such behavior requires that a high proportion of agents lies to sustain the indifference conditions. Conversely, as φ approaches $\mathbb{E}(t)$, every liar will report K , which is only possible if a small proportion of agents lies.

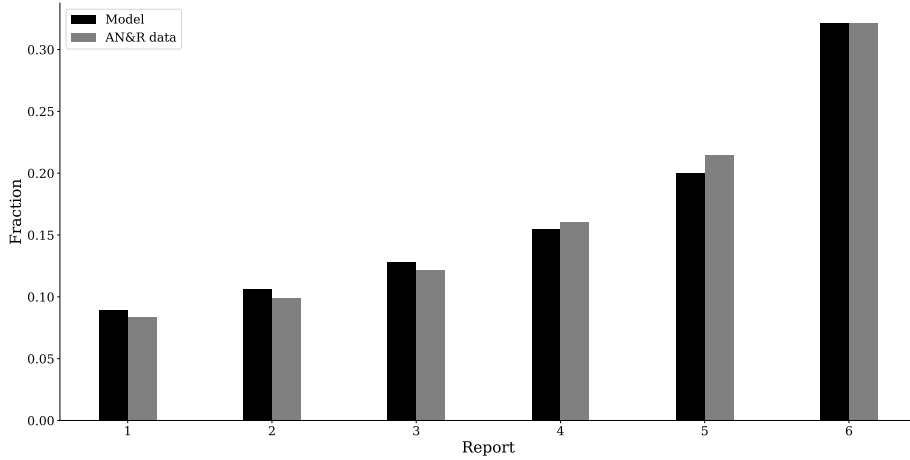
Supply and demand have to coincide in equilibrium, which determines φ^* , which in turn pins down the equilibrium \hat{t}^* , r^* , and k^* . The conditions imposed on $F(t)$ ensure existence.

Equilibrium behavior is shaped by signaling motives and a number of insights follow:

Reporting in equilibrium The equilibrium predicts a report density that is increasing in the direct payoff. We would obtain the same prediction from a model with only intrinsic lying costs. The key difference between both models is however, that, when they are image concerned, some agents might lie and report a non-payoff maximizing state. For example, the model can match the empirical findings from die roll games in laboratory experiments quite well. Figure 3 compares the predicted equilibrium distribution for a calibrated version of the model to the data collected by AN&R. The model comes close to the observed frequency distribution and in particular can account for partial lying.

Freeriding on reputation Liars report a state different from the highest state only if

Figure 3. Example equilibrium report distribution compared to the AN&R data



Note: Example equilibrium distribution of reports when lying costs follow a log-normal distribution where log-costs have mean zero and standard deviation 1.1, for values $y(a) - y(a - 1) = 1$, and $\mu = 2.1$.

they get a higher image payoff in return. In equilibrium, honest agents and liars pool, and liars free-ride on the honest agents’ reputation. One necessary condition for this image enhancing effect is that every state which does not maximize direct payoffs, and which is reported by a liar, is also reported honestly by some agents. This also means that partial lying is sensitive to the underlying distribution of draws. In an extreme case where, e.g., the second-highest state has an initial drawing probability of zero, the model predicts that no agent would lie partially to report that state.

Image spoiling mechanisms States that are reported dishonestly suffer a reputational penalty because of two factors; credibility and composition. If a state is reported by many liars, then any single agent reporting that state does not appear to have credibly done so truthfully. Since liars are of a worse moral type than the average agent, the reputation of a state suffers when more liars are reporting it. In addition, the reputation of a state also depends on the kind of liars that are reporting it. Liars are of higher reputation if they have a relatively high moral type. That is, they only lie if there are substantial utility gains from lying that give them good reasons to lie because the alternative would have been worse. The marginal liar in state j , who is of type \hat{t}_j , always has a higher reputation than the inframarginal liars, who are of expected type $\mathcal{M}^-(\hat{t}_j)$. This implies that the expected type of liars increases in their proportion. In the limit as $\hat{t}_j \rightarrow \bar{t}$, then $\mathcal{M}^-(\hat{t}_j) \rightarrow \mathbb{E}(t)$; there is no stigma associated with liars from state j . This reflects that bad behavior can be normalized because “everybody is doing

it”. If almost all agents are committing the bad deed, then doing so oneself is no longer a sign of low character, but merely a signal of mediocrity.

3 Determinants of reputation: credibility and composition

Let us in this section delve deeper into the determinants of social image. This is crucial to sharpen our intuitions about how image concerns determine behavior. Image concerns lead to strategic interdependencies between agents through the effects agents’ actions have on equilibrium reputations. We will examine these strategic interactions by shifting the type of the marginal liar and evaluating behavioral spillovers.

3.1 The two-state case

I build up intuition for the results by focusing on the case with only two states. Similar results are later derived for $K > 2$ states. From Proposition 2, we know that with two states there is an equilibrium in which agents always tell the truth after drawing 2 and where some agents lie after drawing 1.¹³ Lying brings a direct gain $\Delta(2, 1)$ at a cost of t . In equilibrium, a fraction $F(\hat{t})$ lies after drawing 1. The probability that an agent reporting 2 is truth-telling is $r(\hat{t}) = 1/(1 + F(\hat{t}))$. Reporting 2 over 1 comes with a reputational penalty of size

$$\Psi(t) = \underbrace{\mathcal{M}^+(t)}_{\text{Reputation from reporting 1}} - \underbrace{[r(t)\mathbb{E}(t) + (1 - r(t))\mathcal{M}^-(t)]}_{\text{Reputation from reporting 2}}.$$

I will refer to this function as the *stigma function*. In the two-state case, the equilibrium is pinned down by the threshold type \hat{t} who is exactly indifferent between lying and truth-telling;

$$\Delta(2, 1) - \hat{t} = \mu\Psi(\hat{t}).$$

¹³With $K = 2$ we do not need the symmetric lying strategies refinement to obtain uniqueness.

The left hand side is decreasing in t . Now consider the right hand side. For small values of t , the stigma function goes to zero as

$$\lim_{t \rightarrow 0} \Psi(t) = \mathcal{M}^+(0) - r(0)\mathbb{E}(t) - (1 - r(0))\mathcal{M}^-(0) = \mathbb{E}(t) - \mathbb{E}(t) = 0.$$

As t increases, the stigma changes because of changes in *credibility* of the report and in the *composition* of the agent types who report 1 and 2;

$$\Psi'(t) = \underbrace{\mathcal{M}^{+'}(t) - (1 - r(t))\mathcal{M}^{-'}(t)}_{\text{Composition effect } (\leq 0)} + \underbrace{r'(t)(\mathcal{M}^-(t) - \mathbb{E}(t))}_{\text{Credibility effect } (> 0)}.$$

More agents reporting 2 makes it less credible that anyone reporting 2 is truth-telling. The credibility effect leads to an increase in the stigma of reporting 2 after a marginal increase in t . This is the signaling channel that deed-based models focus on. In the character-based model, we also have to consider that the types of liars changes. The sign of this additional composition effect is ambiguous. The following result however shows that, independently of the sign of the composition effect and for a relatively broad class of distribution functions, the stigma function strictly increases with t .¹⁴ This implies that, with only two states, an increase in aggregate lying (an increase in \hat{t}) increases the stigma of lies (increases $\Psi(\hat{t})$). Lies are strategic substitutes; an increase in lying of one agent crowds out lying of other agents. An equilibrium obtains where the stigma function crosses the direct payoff as displayed in Figure 4.

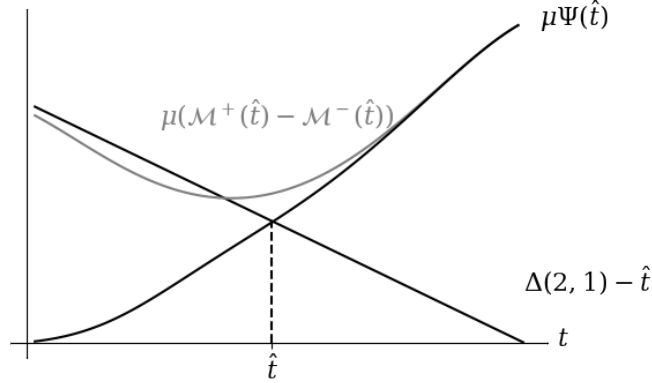
Proposition 3a. *Suppose that $f(t)$ is strictly decreasing or log-concave. The stigma function $\Psi(t)$ is increasing. Lies are strategic substitutes.*

Relation to the honor-stigma model That the stigma function increases with t is distinct from the standard B&T honor-stigma model. In these models, actions are usually perfectly observed so that the reputational stigma from taking the “bad” over the “good” action is equal to $\mathcal{M}^+(\hat{t}) - \mathcal{M}^-(\hat{t})$.¹⁵ In case of a single-peaked type distribution, this difference is decreasing for small t and increasing for larger t . Agents thus face

¹⁴The result holds for all strictly decreasing distribution functions and for the family of log-concave distributions (e.g., the (truncated) normal, exponential, or uniform distributions). Log-concavity is a very common assumption in the signaling literature and the mathematical properties of log-concave distributions are well understood (see [Bagnoli and Bergstrom, 2005](#), for an overview).

¹⁵Most closely related is [Bénabou and Tirole \(2006\)](#), who provide a brief discussion of behavior under forced abstention of some agents (see their Proposition 7).

Figure 4. Equilibrium for $K = 2$



the highest signaling incentives when the marginal type is either very small or very large. As [Adriani and Sonderegger \(2019\)](#) note, this intuitively happens because agents either want to separate themselves from the few “bad apples” that exist in the left tail of the distribution or because they want to belong to the “stars” in the right tail of the distribution. Contrast this with the stigma function in the lying case, which can be rewritten as¹⁶

$$\Psi(t) = 2(1 - r(t))(\mathcal{M}^+(t) - \mathcal{M}^-(t)).$$

In the lying setting, the reputational wedge of the honor-stigma model gets weighted by the probability that a report of 2 is a lie, which reflects the uncertainty about the draw that remains after observing a report of 2. Intuitively, a small amount of “bad apples” barely affects the credibility of reporting 2 and provides agents with weak image incentives to separate to signal honesty. Put another way, truth-telling reputationally only pays off if the observer expects many agents to lie. Figure 4 contrasts signaling incentives in a lying game with signaling incentives in an observed game where the observer can perfectly identify lies. The equilibrium threshold in the lying game is always larger than the threshold in the observed game because identified liars cannot reputationally benefit from pooling with truth-tellers.

¹⁶To see this, use the martingale property of beliefs, $\mathbb{E}(t) = F(t)\mathcal{M}^-(t) + (1 - F(t))\mathcal{M}^+(t)$, to replace $\mathbb{E}(t)$ in the stigma function:

$$\begin{aligned} \Psi(t) &= \mathcal{M}^+(t) - r(t)(F(t)\mathcal{M}^-(t) + (1 - F(t))\mathcal{M}^+(t)) - (1 - r(t))\mathcal{M}^-(t) \\ &= \left(\frac{1 + F(t)}{1 + F(t)} - \frac{1 - F(t)}{1 + F(t)} \right) \mathcal{M}^+(t) - 2(1 - r(t))\mathcal{M}^-(t) \\ &= 2(1 - r(t))(\mathcal{M}^+(t) - \mathcal{M}^-(t)). \end{aligned}$$

3.2 More than two states

We extend the analysis to more than two states. In this case, we can ask how a marginal increase in \hat{t}_k changes the behavior of agents who draw a state j different from k . Other states are affected by increases in \hat{t}_k because such increases have an impact on the image payoff from lying. If the reputation of the highest state increases in response to an increase in \hat{t}_k , then agents from other states will be encouraged to lie. Otherwise, they will be discouraged. The formal results from the two-state case quite naturally extend:

Proposition 3b. *With $K > 2$, lies are strategic substitutes with respect to the k th state if and only if*

$$\omega_k \equiv \underbrace{(1 - \tilde{r}(\hat{\mathbf{t}}^*)) \frac{\partial \mathcal{L}}{\partial \hat{t}_k}}_{\text{Composition effect } (\leq 0)} + \underbrace{\frac{\partial \tilde{r}}{\partial \hat{t}_k} (\mathbb{E}(t) - \mathcal{L}(\hat{\mathbf{t}}^*))}_{\text{Credibility effect } (< 0)} < 0,$$

where

$$\tilde{r}(\hat{\mathbf{t}}) \equiv \frac{1}{K} \frac{1}{\sum_{j \in \mathcal{H}} \alpha_j^* P(\text{report } j)}.$$

The proposition shows that, similarly to the two state case, credibility and composition effects guide behavior when there are multiple states. To better see this, consider the expected credibility of a liar's report. In an equilibrium with partial lying, liars play mixed strategies, where they, conditional on lying, report a state j with probability α_j . Bayes' rule tells us that the credibility of any report of a high state is $P(\text{truth}|j) = 1/K \times 1/P(\text{report } j)$. Therefore, the expected credibility a liar will get is

$$\mathbb{E}_{\alpha_j}(P(\text{truth}|\text{report } j)) = \frac{1}{K} \sum_{j \in \mathcal{H}} \alpha_j^* \frac{1}{P(\text{report } j)},$$

which is approximately equal to the $\tilde{r}(\hat{\mathbf{t}})$ in the proposition.¹⁷

Differently from the two-state case, strategic complementarities can obtain. An increase in \hat{t}_1 will always lead to a positive composition effect; if this positive effect dominates the credibility effect strategic complementarities obtain. The composition effect is smaller for larger k and can be negative if $t_k > \mathcal{L}(\hat{\mathbf{t}})$, e.g., after an increase

¹⁷In an equilibrium without partial lying both terms exactly coincide since $\alpha_K = 1$. The reason that they do not coincide when there is partial lying is that the α_j s themselves change after an exogenous increase in \hat{t}_k .

in \hat{t}_{k^*} . Intuitively, only the lowest moral types would lie after drawing k^* while also higher types would lie after drawing 1. Liars from k^* are relatively cheap; they lie for a smaller utility gain than liars from 1, which makes them the liars with the lowest average reputation.¹⁸ Another element that contributes to strategic complementarity is the baseline lying rate. If lying already is on a high level (so that $1 - \tilde{r}(\hat{t}^*)$ is large) the composition effect gains in weight and actions are more likely strategic complements.

4 Applications

This section considers two applications of the model. We first consider the role of beliefs about others on behavior. Thereafter, we will turn to the effects of different forms of lie detection and disclosure.

4.1 Changing beliefs

Agents in the model prefer appearing as a high type over appearing as a low type. The size reputational stigma of making a dishonest report closely depends on the distribution of types and on beliefs that agents and the observer hold about it. This part asks how a change in beliefs about the type distribution affects behavior.

One interpretation of the following comparative statics is to think of moving a single agent of a given type from a population with a certain preference distribution to a population with a different preference distribution and asking how the agent adjusts their behavior (see, e.g., [Adriani and Sonderegger, 2019](#)). However, the comparative statics also apply if we are willing to entertain a non-equilibrium solution concept where agents best respond to their subjective second-order belief about the observer's belief about the type distribution. Seen in this light, a comparative static that shifts a moment of the preference distribution can be more literally interpreted as a shift in the agent's second order belief. Such shifts might occur after a norms-based interven-

¹⁸The fact that “small” lies are more severely stigmatized than “large” lies would be more ambiguous in a setting where agents' lying decisions have direct payoff implications for a third party. In settings where agents cheat at the expense of others, it would be appropriate to introduce further moral dimensions, such as pro-sociality, into the model. The consequence might be that a “large” lie is more stigmatized than a “small” lie, because agents who take from someone else signal that they care little about the welfare of others. (See e.g. [Cohn, Maréchal, Tannenbaum, and Zünd \(2019\)](#) for further discussion and evidence that individuals are less likely to cheat for a large gain than for a small gain when they believe that someone else will suffer from it.)

tions which aims to correct agent’s misperceptions about average behavior (Bénabou and Tirole, 2011). Alternatively, following Bénabou, Falk, and Tirole (2020),¹⁹ shifts in agents’ second-order beliefs could be brought about by third parties who persuade agents to hold a certain belief about the preference distribution by using narratives. I will use the narrative analogy in the first two comparative statics I will discuss. An additional interpretation which will be provided for the last comparative static in this section is that myopic agents and an observer repeatedly interact, with the observer’s prior about agents’ characters becoming more precise over time.

4.1.1 The two state case

We again build up the basic intuition with two states. Throughout this section, we will assume that the conditions of Proposition 3a hold so that $\Psi(t)$ is increasing.

A “nobody is perfect” narrative Consider agents who are exposed to a narrative that almost “nobody is perfect” and might lie at some point. We can think about this narrative as leading to a shift in the belief about the prior type distribution function, redistributing some probability mass out of the right tail of the distribution (i.e., the part where the highest moral types are located) to the left tail. One way to model this is by reducing the highest type \bar{t} to a lower one, $\tau < \bar{t}$ (while maintaining the assumption that $\tau > \Delta(2, 1) + \mu\mathbb{E}(t|t \leq \tau)$ to focus on interior equilibria).²⁰

A reduction in \bar{t} will affect the marginal type who is indifferent between truth-telling and lying through the stigma function $\Psi_{\bar{t}}(t)$. We will denote the stigma function under the new, right-truncated distribution (see the left panel in Figure 5) as

$$\Psi_{\tau}(\hat{t}) = \mathcal{M}_{\tau}^{+}(\hat{t}) - [r_{\tau}(\hat{t})\mathbb{E}_{\tau}(t) + (1 - r_{\tau}(\hat{t}))\mathcal{M}_{\tau}^{-}(\hat{t})].$$

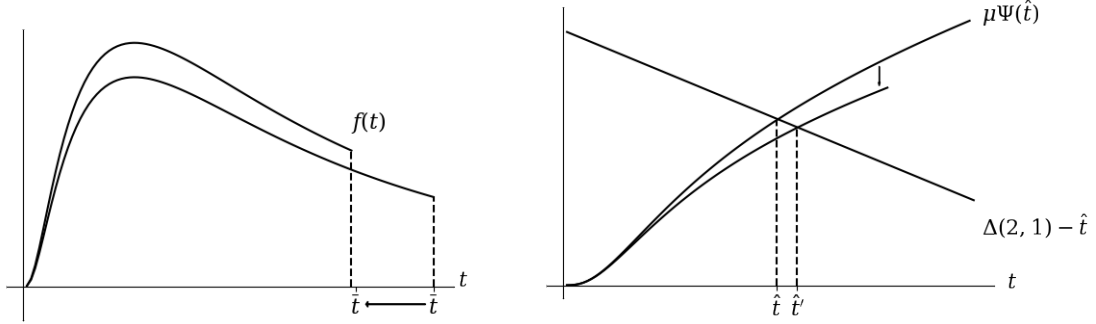
In the equation above, the τ subscripts indicate the new truncation point.²¹ To inves-

¹⁹Bénabou et al. (2020) study a case where narratives can shift agents’ beliefs about the size of the externality of an action they take, while I look at narratives which shift agents’ beliefs about the type distribution. The paper by Bénabou et al. (2020) is part of a emerging recent literature that investigate the effect of narratives on behavior. Other related papers are Eliaz and Spiegel (2020), Foerster and van der Weele (2021), and Schwartzstein and Sunderam (2021). Golman (2021) fully specifies the equilibrium of a game where agents express potentially controversial opinions and tailor interpretations of past data to increase their reputational utility in front of others.

²⁰If the reduction in \bar{t} is larger, agents might expect everyone to lie after the reduction. Psychological versions of the intuitive criterion exist which could be used to pin down off-equilibrium beliefs in such a situation (Bernheim, 1994, Dufwenberg and Lundholm, 2001).

²¹That is, $\mathbb{E}_{\tau}(t) = \mathbb{E}(t|t \leq \tau)$, $\mathcal{M}_{\tau}^{+}(\hat{t}) = E(t|t \in (\hat{t}, \tau))$, $r_{\tau} = 1/(F(\tau) - F(\hat{t}))$. Note that $\mathcal{M}_{\tau}^{-}(\hat{t}) = \mathcal{M}^{-}(\hat{t})$

Figure 5. Effect of a decrease of \bar{t}



to investigate the effect of truncating the belief distribution, consider the derivative of $\Psi_\tau(\hat{t})$ with respect to τ ;

$$\frac{\partial \Psi_\tau(\hat{t})}{\partial \tau} = \underbrace{\frac{\partial \mathcal{M}_\tau^+(\hat{t})}{\partial \tau} - r_\tau(\hat{t}) \frac{\partial \mathbb{E}_\tau(t)}{\partial \tau}}_{\text{Composition effect } (> 0)} + \underbrace{\frac{\partial r_\tau}{\partial \tau} (\mathcal{M}_\tau^-(\hat{t}) - \mathbb{E}_\tau(t))}_{\text{Credibility effect } (< 0)}.$$

Again we see by now familiar credibility and composition effects. Going from \bar{t} to τ decreases the stigma of lying decreases through the composition effect because, after knowing that “nobody is perfect”, the reputation of truth tellers is stained. At the same time, the reputation of liars remains unaffected, as they are exclusively drawn from the left tail of the distribution. In the present case, the composition effect always dominates the credibility effect. Therefore, a decrease in \bar{t} shifts the stigma function downwards. As illustrated in the right panel of Figure 5, agents become more likely to lie.

Proposition 4a. *If $f_X(t)$ is a density function with $f_X(t) > 0$ for $t \in (0, \bar{t}]$ and $f_Y(t)$ is a version of $f_X(t)$ truncated at a point τ , where $\Delta(2, 1) + \mu \mathbb{E}(t|t \leq \tau) < \tau < \bar{t}$, then agents with belief $f_Y(t)$ are more likely to lie than agents with belief $f_X(t)$.*

An agent who decreases their parameter belief of the top type from \bar{t} to τ becomes more likely to lie. Decreasing \bar{t} also has the effect that the agent now believes that a higher fraction of other agents are lying (since none of them is of a very high type). As the next result shows, it is however not generally true that an increase in the belief about the proportion of others lying increases one’s own propensity to lie.

Shifting the preference distribution to the right Consider shifting the whole belief density function $f_X(t)$ to the right using a positive parameter a so that $f_Y(t) = f_X(t - a)$.

as long as $\hat{t} \leq \tau$.

Such a shift results in agents believing that other agents are more honest as probability mass is shifted away from low moral types towards high types. Differently from the last comparative static, this shift happens for the whole distribution. Agents therefore come to believe that other agents are less likely to lie than before, making a high report more credible. This credibility effect dominates in the present case, so that agents become more likely to lie.

Proposition 4b. *If $f_X(t)$ is a density function with $f_X(t) > 0$ for $t \in (0, \bar{t}]$ and $f_Y(t)$ is a version of $f_X(t)$ with $f_Y(t) = f_X(t - a)$ where $a > 0$ then agents with belief $f_Y(t)$ are more likely to lie than agents with belief $f_X(t)$.*

Even though the belief changes examined in the previous two comparative statics have seemingly opposite consequences—in the first, the agents come to believe that more other agents will lie while in the second agents come to believe that fewer other agents will lie—both comparative static results predict that agents themselves become more likely to lie after shifting their belief. This happens because the composition effect dominates in the first comparative static comparison while the credibility effect dominates in the second comparative static comparison.

Can we apply these insights to a setting that is not as stylized as in the model? In reality, it would be difficult to measure the underlying preference distribution and beliefs about it. However, it sometimes is possible to observe past actions of others, be it by measuring lying in the lab and exposing future participants to that data or by estimating, e.g., the level of tax income misreporting from household consumption data. If evidence of high levels of cheating is interpreted as evidence that truth-telling is not very diagnostic of honor (as in the “nobody is perfect” narrative), this reduces truth-telling. If an interpretation of the same data instead makes individuals aware of the high level of suspicion they will raise by making a report that is made by an implausibly high number of individuals, then it will increase truth-telling. We might thus expect different actors making arguments that either justify lying by claiming that others would have behaved in the same unethical way in a similar situation or that encourage truth-telling by stressing the incredibility of high reports.

The role of type uncertainty Consider an observer who knows the past history of agents’ actions, which she can use to reduce her prior uncertainty about the agents’ types. How do agents adjust their behavior to the observer’s new beliefs? To study the role of changing uncertainty about types, we will compare behavior under two type

distributions that can be ordered according to the Unimodal Likelihood Ratio order, which was introduced by [Ramos, Ollero, and Sordo \(2000\)](#):

Definition 3. *Two distributions $F_X(t)$, $F_Y(t)$ satisfy the Unimodal Likelihood Ratio (ULR) order if the likelihood ratio $f_X(t)/f_Y(t)$ is unimodal and $\mathbb{E}_X(t) \geq \mathbb{E}_Y(t)$.*

The ULR order is a measure of the relative dispersion of probability distributions: The results of [Ramos et al. \(2000\)](#) imply that, if two distributions satisfy ULR and have the same mean, then $F_Y(t)$ is a mean-preserving spread of $F_X(t)$.²² Comparing behavior under different type distributions which can be ordered according to ULR and whose mean coincides therefore addresses the question of changing type uncertainty. To anticipate the intuition behind the following comparative static, think about adding noise to an initial type distribution. The resulting more dispersed distribution will have fatter left and right tails than the initial distribution. As a consequence, the conditional expectations $\mathcal{M}^+(t)$ and $\mathcal{M}^-(t)$ will take on more extreme values under the more dispersed distribution. This in turn increases the stigma of reporting 2 instead of 1 for a given threshold type, which leads to the following result.

Proposition 4c. *Suppose the distributions $F_X(t)$ and $F_Y(t)$ satisfy the ULR order, that $\mathbb{E}_X(t) = \mathbb{E}_Y(t)$, and that both densities have full support on $(0, \bar{t}]$. Then agents with belief $f_Y(t)$ are less likely to lie than agents with belief $f_X(t)$.*

In the character-based model, agents want to convince the observer that they are of a high type. As the observer's prior becomes more certain, agents have less room to move the observer's prior by taking any particular action. Their actions in turn are less guided by image concerns, which makes them more likely to lie.

Comparison to deed-based image I relate the findings to those of a deed-based model in which agents are esteemed for taking an honest action. In such a model, agents receive a reputation that is proportional to the probability that they made a truthful report. For example, in [GK&S's](#) model the stigma function would be

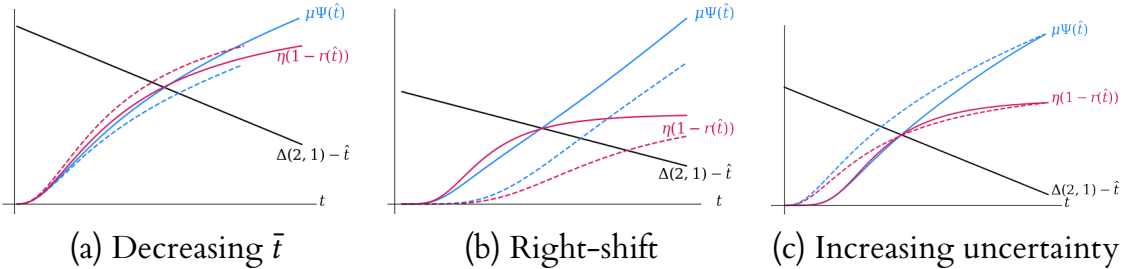
$$\Psi^D(t) = P(\text{truth}|\text{report } 1) - P(\text{truth}|\text{report } 2) = 1 - r(t).$$

It only depends on a credibility effect. Any change in the preference distribution which decreases agents' beliefs about the likelihood that others lie decreases the stigma of

²²The ULR is a sufficient condition for second-order stochastic dominance that is fulfilled by many families of distributions. For example, within the family of normal or lognormal distributions, ULR and second-order stochastic dominance are equivalent conditions ([Hopkins and Kornienko, 2007](#)).

reporting 2. Stigma increases otherwise. This leads to some contrasting predictions between both models, as displayed in Figure 6. In the deed-based model, redistributing probability mass from the right tail to the left tail of the distribution through a reduction in \bar{t} makes agents aware that reporting 2 has low credibility, therefore decreasing lying. This prediction is opposite to the character-based model. Qualitative predictions of both models coincide when considering a right-shift in the distribution, where they predict a decrease in stigma.

Figure 6. Comparative statics of deed- and image-based models



Note: Solid lines display stigma functions in the character-based (blue line) and deed-based (red line) models. Dashed lines display comparative statics of, respectively, decreasing \bar{t} , shifting the preference distribution to the right, and increasing the uncertainty of the preference distribution. The image weight in the deed-based model, η , was calibrated in such a way that the initial threshold type \hat{t} always coincides.

The deed-based model does not make a clear prediction about how changing uncertainty about preferences affects behavior. Thus, signaling incentives in the deed-based model do not necessarily become weaker as the observer learns about agents from their past actions. There is an interesting connection between this last comparison and the influential criminological theory by Braithwaite (1989) (see also Makkai and Braithwaite, 1994). Braithwaite distinguishes between reintegrative and disintegrative shaming. Shaming is reintegrative if it condemns a moral transgression but does not make inferences about personal traits of the transgressor based on the transgression (what we may call deed-based). Shaming is disintegrative if it generalizes from transgressions to personal traits of the transgressor (what we may call character-based). In his theory, disintegrative shaming leads to worse outcomes as transgressors are labeled as deviants and expectations about their deviant character stay attached to them. Transgressors in turn become more likely to re-offend. The comparison between the character- and deed-based models may be seen as giving a formal rationale for that distinction. The point is that in a population that mostly focuses on character-based image, signaling

incentives, and thus truth-telling, decreases as observers form more precise priors.²³

4.1.2 More than two states

With more than two states, we have to account for the effect that liars from different states respond to changes in the belief distribution on different margins. This triggers an additional equilibrium effect. The sign of this additional effect can either be positive or negative depending on whether actions from different states are strategic substitutes or complements. The proposition below states a general result for changing a generic parameter θ of the belief distribution.

Proposition 4d. *Consider a family of belief distributions $f_\theta(t)$ which is characterized by a parameter θ . A marginal increase in θ decreases lying from a state k if and only if*

$$(\tilde{r}(\mathbf{t}^*)\xi + (1 - \tilde{r}(\mathbf{t}^*))) \frac{\partial \mathcal{M}_\theta^+(\hat{t}_k^*)}{\partial \theta} - \tilde{r}(\mathbf{t}^*)\xi \frac{\partial E_\theta(t)}{\partial \theta} - (1 - \tilde{r}(\mathbf{t}^*)) \frac{\partial \mathcal{L}}{\partial \theta} + \frac{\partial \tilde{r}}{\partial \theta} (E_\theta(t) - \mathcal{L}_\theta(\mathbf{t}^*)) > \sum_{j \in \mathcal{K}} \omega_j(\hat{\mathbf{t}}^*) \frac{\partial \hat{t}_j}{\partial \varphi} \left(\frac{\partial \mathcal{M}_\theta^+(\hat{t}_k^*)}{\partial \theta} - \frac{\partial \mathcal{M}_\theta^+(\hat{t}_j^*)}{\partial \theta} \right),$$

where

$$\xi = \tilde{r}(\mathbf{t}^*) \sum_{j \in \mathcal{K}} \alpha_j^2 (K - k^*) + (1 - \tilde{r}(\mathbf{t}^*)) \quad (\approx 1)$$

and \tilde{r} and ω_j are defined as in Proposition 3b.

The left-hand side of the condition above is a version of the derivative of the stigma function generalized to K states. The right-hand side denotes additional second-order equilibrium effects, whose sign and size are indeterminate unless we make specific assumptions about $f(t)$ and which becomes relatively irrelevant as μ becomes smaller.²⁴

²³Experimental evidence suggests that lying becomes more prevalent in repeated environments. In their meta study, AN&R report a small, but significantly positive, coefficient of the round of repetition on reporting. However, there are at least two concerns with interpreting this finding as being consistent with the character-based model: First, experimental participants usually know in advance that they will repeat the lying task and it is not clear how forward-looking their behavior is. Second, the experimenter typically inspects the report sequences only after the experiment, so that it would be wrong to think of the experimenter as an observer who updates her belief after every single report.

²⁴For example, if $f(t)$ is uniform then the r.h.s. is zero. The smaller μ the smaller the second-order behavioral reaction which appears on the r.h.s. through $\partial t_j / \partial \varphi$.

4.2 Verification and disclosure of lies

If individuals care about their image, they should react to threats of being verified and publicly exposed as a liar. This has motivated authors to promote raising the salience of caught lies in the policy mix to increase honesty (e.g., [Abeler et al., 2019](#)). Such policies are, for example, already used by some US States who maintain publicly accessible websites which list the names and addresses of individuals who accumulated tax debt ([Perez-Truglia and Troiano, 2018](#)). With character-based image, agents are sensitive to how their lies will be disclosed after verification. This section discusses how the type of disclosure policy might matter.

Consider an additional player in the game, the investigator. After reports are made, the investigator detects the original draw of any agent with probability π and discloses lies to the observer. In its most basic form, the investigator could rely on *coarse disclosure* that discloses lies, but not the original draw of the liar. Such a regime results in an image of $\mathcal{L}(\hat{t})$ for a disclosed liar. The expected reputation of a liar reporting K then becomes

$$\varphi^{cd} = (1 - \pi)[r_K \mathbb{E}(t) + (1 - r_K) \mathcal{L}(\hat{t})] + \pi \mathcal{L}(\hat{t}).$$

As they gain a lower reputation when disclosed as a liar, agents prefer not being disclosed as a liar to being disclosed. Introducing verification and disclosure thus reduces lying. It also makes partial lying less attractive as partial liars are as likely as full liars to be caught lying, so that the reputational advantage of partial over full-extent lying becomes smaller.²⁵

Proposition 5a. *After an increase in the probability of lie detection π*

- (i) *The threshold state k^* weakly increases.*
- (ii) *The likelihood that an agent lies decreases.*

Assume for the rest of the section that the prior type distribution is uniform.²⁶ Since the investigator observes the state originally drawn by the liar, they could additionally commit in advance to disclosing it with some probability γ . Such *contextualized disclosure* would result in an image of $\mathcal{M}^-(\hat{t}_j)$ for caught liars. Consider going from the

²⁵An interesting extension of the model could consider an investigator who, faced with a distribution of reports, can choose to verify a fixed fraction of reports. If the goal is to maximize the lie detection rate the investigator should disproportionately focus on investigating reports of the highest state. This could, contrary to the present result, encourage partial lying.

²⁶This is mainly for ease of exposition. Similar results can be derived for different distributions.

coarse to the contextualized regime. Liars from the lowest states, with a moral type larger than the average liar, will prefer contextualized disclosure to coarse disclosure. They become more likely to lie. However, liars from higher states, who have a type smaller than the average liar, will dislike contextualized disclosure as they can no longer benefit as much from being pooled with the liars from the lowest states upon detection. They become less likely to lie. These first-order effects lead to an increase in the average size of the lie.

Now consider an agent who draws one of the lowest states. The direct effect of introducing the contextualized disclosure regime encourages them to lie because they can separate from other liars in case of disclosure. Albeit this direct effect is there, it is also relatively small; agents from the lowest states are overrepresented among liars, so conditionally on being disclosed as a liar already under coarse disclosure it is likely that they drew a low state. In contrast, the reputational penalty of going to contextualized disclosure is relatively harsher for agents from higher states as they only constitute a minority of liars. Therefore, the direct effect of going to contextualized disclosure will have a larger behavioral effect on “small” liars who reduce their lying, than on “large” liars who increase their lying.

Choosing between coarse or contextualized disclosure thus constitutes a tradeoff between minimizing the total lying rate and the average size of lies.

Proposition 5b. *Suppose that lies are detected with probability $\pi > 0$ and that $t \sim U(0, \bar{t})$. After an increase in the probability of disclosing the initial draw γ*

- (i) *The average size of lies increases.*
- (ii) *The lying rate decreases.*

Relation to deed-based image While a larger verification probability decreases lies also in the deed-based model, the type of disclosure regime will not affect behavior. This is the case because the observer does not differentiate between different types of liars. Therefore, providing additional context about the disclosed liar does not influence the observer’s judgement.

5 Extensions

This section considers two extensions that change two assumptions on preferences that we maintained throughout the main text: fixed lying costs and a homogenous image concern.

5.1 Increasing lying costs

This part considers the robustness of the results to possible generalizations of the lying cost function. Consider a more general case of agents' utility function:

$$u(j, t, a) = y(a) - c(j, t, a) + \mu\mathcal{R}_a.$$

In the main part we considered fixed lying costs where $c(j, t, a) = t$. GK&S and K&S provide results for the case of a deed-based model with lying costs consisting of a fixed, moral type-dependent and a variable, moral type-independent component. For example, K&S study the case where $c(j, t, a) = t + \kappa|a - j|$. They show that all equilibrium features of the deed-based model remain qualitatively the same; introducing the variable cost changes how participants trade off full and partial lying on the margin (a higher variable cost parameter κ makes partial lying relatively more attractive) but does not lead to a qualitatively different equilibrium. It is relatively straightforward to show that the same results translate to our setting. As long as variable lying costs do not depend on the moral type, they will not fundamentally change equilibrium behavior.

To study another potentially interesting case, in this part I consider behavior under type-dependent increasing lying costs of the form $c(j, t, a) = t|a - j|$. Here, the moral type now determines the slope of the lying cost function, with higher types facing a steeper slope. There are two reasons why increasing lying costs can lead to partial lying. First, with increasing lying costs, agents might prefer to tell a partial lie for purely intrinsic reasons. For example, if the direct payoff function $y(a)$ is strictly concave, then there might be agents whose payoff gain outweighs the moral cost when telling a small lie (going from 1 to 3), but not when telling a large lie (going from 1 to 6). Second, increasing lying costs might interact with the image concern to motivate agents to lie partially. To be able to cleanly state how signaling motives change agents' lying behavior under increasing lying costs, we will in this part assume that $y(a) = a$. This establishes an easily comparable benchmark; if lying costs and direct payoffs are linear

functions, then absent image concerns, agents either lie to report K or tell the truth. If we set $\mu = 0$, agents will lie if and only if $t \leq 1$ and $j < K$. If they lie, they will report K .

We can now ask how behavior is different with image concerns, i.e., when $\mu > 0$. Suppose that an equilibrium exists where every liar reports K . In such an equilibrium, a larger fraction must lie after drawing 1 than after drawing $K - 1$. This implies two things; first, the marginal liar from state $K - 1$ is indifferent between reporting K and $K - 1$. Second, the marginal liar from state 1 is indifferent between reporting K and 1. Taken together, both facts imply that the marginal liar from 1 is of a higher moral type than the marginal liar from $K - 1$. A consequence is that the marginal liar from 1 will prefer reporting $K - 1$ over K , a contradiction:

Proposition 6a. *With lying costs $c(t, j, a) = t|j - a|$, $y(a) = a$, and $\mu > 0$ and if $K > 2$, there is no equilibrium in which liars only report K .*

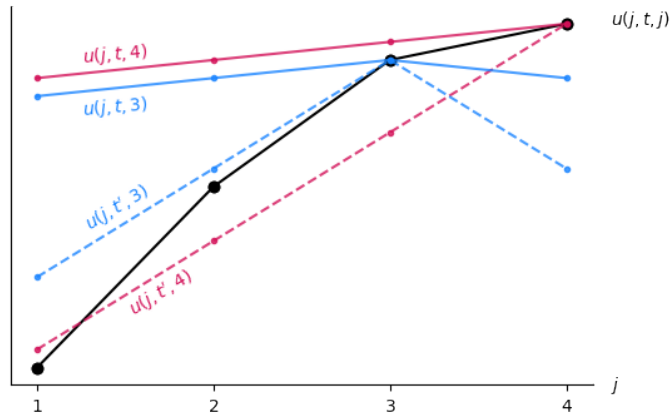
In contrast to the no-image benchmark, variable lying costs predict an equilibrium with a lot of partial lying. In this equilibrium, agents who draw j will report any number between $j + 1$ and K if they lie—which number they exactly report depends on their moral type. The least moral types report K , followed by slightly more moral types reporting $K - 1$ and so on:

Proposition 6b. *When lying costs are of the form $c(t, j, a) = t|j - a|$, $y(a) = a$, and $\mu > 0$, there is an equilibrium which is characterized by the threshold types $1 > \hat{t}_1 > \dots > \hat{t}_{K-1} > \hat{t}_K = 0$. In equilibrium, agents of type (j, t) will lie and report k if and only if $j < k$ and $t \in (\hat{t}_k, \hat{t}_{k-1}]$.*

The equilibrium thus predicts that, in equilibrium, every state larger than 1 is reported by a liar with positive probability. The extreme prediction follows from the interaction between image concerns and increasing lying costs: With a nonzero image weight, the truthful reporting utility becomes strictly concave in the reported state. As a consequence, the marginal utility difference from reporting $j + 1$ over j becomes smaller as j increases. Therefore, it becomes optimal for some moral types to lie to report a smaller number than K . Figure 7 illustrates this dynamic by plotting the equilibrium utility received from truth-telling and lying for selected types in a game with $K = 4$. The black line plots the utility that agents receive from truthfully reporting j . The red lines plot the utility that agents of moral types t and t' receive when they

report 4, with $t < t'$. Increasing t causes the red line to pivot downwards, as higher moral types face a steeper slope of the lying cost. The red lines also show that the type t prefers lying and reporting 4 to truth-telling after drawing a number smaller than 4 (the solid red line is above the black line). Type t' on the other hand only prefers lying to 4 over truth-telling after drawing 1. The blue lines in the figure plot the equilibrium utility that types t and t' receive after reporting 3. They show that type t prefers reporting 4 to reporting 3 after drawing any state (the solid red line is above the solid blue line) while t' prefers reporting 3 to reporting 4 after drawing a number smaller than 4 (the dashed blue line is above the dashed red line left of $j = 3$). There is also no downwards lying as no type will ever receive a utility value from lying downwards that is larger than the utility value from truth-telling.

Figure 7. Equilibrium with increasing lying costs and $K = 4$



Some experimental evidence exists that casts doubts on the equilibrium prediction of the increasing lying costs model. GK&S, for example, report that, in an observed lying game where participants can report numbers between 1 and 10, almost no individual dishonestly reports a number smaller than 9. In the observed game, only the composition effect of the character-based model is active but this alone is enough to predict an equilibrium in the observed game that has the same qualitative features as the one described in Proposition 6b. That is, it would predict that every state except for 1 is reported dishonestly with positive probability. This prediction, however, is not borne out in the data.

5.2 Heterogenous image concerns

While the paper assumed homogenous image concerns so far, papers such as [Friedrichsen and Engelmann \(2018\)](#) and [Butera, Metcalfe, Morrison, and Taubinsky \(2022\)](#) provide empirical evidence that different individuals care about their image to different extents. When this is the case, and when individuals anticipate heterogenous image concerns in others, behavior might change in meaningful ways. I briefly discuss the implications of heterogenous image concerns in the following.

Suppose agents hold an image concern which is drawn from a distribution $g(\mu)$ which has full support on $[0, \bar{\mu}]$ and which is independent of t . Partial lying will now arise as part of an equilibrium if there is a type with a sufficiently large image concern.

Proposition 7a. *When agents draw their image concern from a distribution $g(\mu)$ with full support between $[0, \bar{\mu}]$ and if $K > 2$, there is no equilibrium where liars only report K if $\bar{\mu}$ is sufficiently large.*

Partial lying thus still emerges under heterogenous image concerns but it will be of a slightly different kind. Remember how in the baseline analysis, liars are indifferent between any state that is reported dishonestly with positive probability in equilibrium. With heterogeneous image concerns this is no longer the case: some agents will value a high image payoff more than others, which leads them to strictly prefer partial to full lying. The resulting equilibrium is one where liars separate by their image type; as the following proposition shows, for an intermediate range of $\bar{\mu}$, the less image concerned liars report K while more image concerned liars report $K - 1$.

Proposition 7b. *Suppose that agents draw their image concern from a distribution $g(\mu)$ with full support between $[0, \bar{\mu}]$. For intermediate parameter values of $\bar{\mu}$ and for $K > 3$, there is an equilibrium which is characterized by threshold types $\hat{\mu} \in (0, \bar{\mu})$, $\hat{t}_{Kj}(\mu)$, and $\hat{t}_{K-1j}(\mu)$. Agents of type (j, t, μ) lie and report K if $\mu \leq \hat{\mu}$ and $t \leq \hat{t}_{Kj}(\mu)$. They lie and report $K - 1$ if $\mu > \hat{\mu}$ and $t \leq \hat{t}_{K-1j}(\mu)$.*

Apart from predicting a separation by image type, the equilibrium above predicts downward lying: An highly image concerned agent will prefer honestly reporting $K - 1$ over honestly reporting K . If their intrinsic lying cost is sufficiently low, they will thus also prefer dishonestly reporting $K - 1$ after drawing K . More extreme versions of the downward lying prediction plausibly exist as $\bar{\mu}$ increases beyond the intermediate

range. For example, in the most extreme case an agent with very high image concern (e.g. $\mu \rightarrow \infty$) has a strict incentive to report 1 after drawing K , even if K is large.

The heterogenous image concerns equilibrium in addition can rationalize report distributions where the modal report is smaller than K . This can happen if there is a positive correlation between an agent's moral type and image concern. Then, the liars who report K because they care little about their image are also those with the lowest moral types, and other liars will dislike pooling with them. If this motive is strong enough, more agents will report $K - 1$ than K in order to avoid making the same report that the worst types make.²⁷ Note that this prediction is exclusive to the character-based model: In such an equilibrium, reporting $K - 1$ is more obviously a lie than reporting K , since more liars report $K - 1$. Such an equilibrium would therefore be impossible in a deed based model. In the character-based model however, if liars reporting $K - 1$ are of a higher moral type than those reporting K , such an equilibrium can be sustained through the composition effect.

There is evidence that the highest state is not always reported by most participants. For example, 8 out of 24 papers included in the [AN&R](#) meta-study that employ a one-shot die-roll lying game contain experiments where the highest state is not the modal report. Most of these experiments have been conducted outside of traditional lab environments in settings where the social distance between observer and participants is arguably lower and where the social image motive thus might play a greater role. For example, [Ruffle and Tobol \(2017\)](#) conduct an experiment with Israeli soldiers who have to report the outcome of a die roll to an army official. The higher the reported die roll, the earlier the soldiers will be released from duty at one weekday afternoon. They find that some soldiers lie to the army official and that most of them report the second-highest state.

6 Related literature

This section provides a discussion of the relation between the model and previous theoretical work. Thereafter, I consider experimental research on image concerns and lying.

²⁷Appendix C presents an example of such an equilibrium.

6.1 Relation to other image models

Agents in the model presented in this paper are motivated by the ethics of virtue, while agents in deed-based models are deontological in the sense that their ethics follows a rule (“you should not lie”). While signaling motives in the deed-based models are only about *credibility* (how suspicious the report is), the character-based model adds a further *composition effect* (what kind of agents are going to lie).

Gneezy et al. (2018) (GK&S) and Khametski and Sliwka (2019) (K&S) fully characterize equilibria in versions of the deed-based model. They derive the result that the report distribution is unique in any equilibrium even though there are typically multiple equilibrium strategy profiles. The current paper derives a uniqueness result after imposing a symmetry refinement that, as was argued, seems relatively weak. It requires agents not to condition their dishonest reports on decision irrelevant aspects. This difference between the models stems from the fact that, in the deed-based models, reputations are type-independent, so that there typically is a one-to-one mapping between the proportion of liars reporting a state and the reputation of that state.²⁸ Imposing symmetric lying strategies in the character-based model reestablishes something similar to type-independence because it ensures that liars reporting any state are of the same expected type.

Abeles et al. (2019) (AN&R) provide a discussion of deed-based signaling under heterogeneous image concerns. They show that downwards lying, where agents lie to report a lower payoff, can arise as part of an equilibrium. This has implications for their comparative statics results for how reporting changes after agents adjust their beliefs about other agents. Consider a two state game where agents increase their belief about the proportion of agents reporting 2. One inference that agents can make after increasing their belief is that the proportion of upward liars from 1 to 2 is higher than they previously expected. As a consequence, reporting 2 becomes less credible. However, reporting 1 also becomes less credible, as due to downward lying, the fraction of truth-telling agents reporting 1 decreases. Whether agents become more or less willing to lie upwards after the belief increase depends on whether the credibility decline of reporting 2 is smaller or larger than the credibility decline of reporting 1. Therefore, in a deed-based model with heterogeneous image concerns agents can become more

²⁸The exception is the model of Dufwenberg and Dufwenberg (2018) in which reputations depend on the size of the lie. This also leads to the emergence of multiple equilibria.

likely to lie after increasing their belief, even though lies are strategic substitutes in the model and the mechanism by which lying increases is different from the mechanism through which beliefs affect decision-making in the character-based model.

[Dufwenberg and Dufwenberg \(2018\)](#) (D&D) consider a setup with no intrinsic lying costs but where image payoffs depend on some perceived cheating aversion which is increasing in the size of the lie that the observer infers to judge the intensity of unethical behavior. Thus, the observer distinguishes between more than a good deed (truth-telling) and a bad deed (lying), by interacting actions with the intensive margin of the lie. This could, for example, be a realistic assumption if observers dislike the deceptive element of a lie, as a large lie (reporting five instead of one) intends to deceive the observer by more than a small lie (reporting four instead of three). As in the character-based model, incorporating an intensive margin leads to reputations that are strictly smaller the higher the report. The observer's motivation is however different; in [D&D](#), the primary motivation of the observer is to distinguish between small and large deeds of cheating, without inferring what the deed tells her about the agent's character.

6.2 Experimental evidence

A number of experimental tests show that deed-based models provide correct predictions about lying behavior in previously untested environments. In one of their experimental treatments, [GK&S](#) reduce the probability with which participants draw, and therefore truthfully can report, the highest state. The theoretical prediction is that a wider range of non payoff-maximizing states is reported because it is less credible that participants truthfully report the highest state. The experimental results are in line with this prediction. In a similar spirit, [AN&R](#) find that participants who draw the lower state in a two-state lying game become less likely to lie when the probability of drawing the high state decreases. [Feess and Kerzenmacher \(2018\)](#) test a related mechanism. In their experiment, they exogenously vary the probability with which participants who toss the lower-paying side of a virtual coin can lie and report the higher-paying side. That is, some participants who toss low can lie while others can not. They find that a smaller proportion of participants lies if there are more participants who have the possibility to lie. This is also consistent with the notion that individuals care about how credible their report is.

The experiments described above change parameters of the game to manipulate participants' credibility beliefs. A second strand of experiments holds the game constant and introduce different measures to shift beliefs. Results from these papers typically provide less direct evidence for deed-based models. In one experiment of that sort, [AN&R](#) measure behavior in a binary lying game where participants hold different beliefs about the fraction of others reporting the high state. They exogenously shift beliefs of participants using an anchoring technique and find that a smaller proportion of participants whose belief was exogenously increased lies. This effect, though insignificant, goes into the direction predicted by the deed-based model.

Other experiments of that kind provide information about past behavior to induce participants to update their beliefs ([Rauhut, 2013](#), [Diekmann, Przepiorka, and Rauhut, 2015](#), [Akin, 2019](#)). These experiments usually find zero average treatment effects that mask heterogeneous responses, where, after being provided with information, underestimators become more likely to lie and overestimators less likely to lie. These observations are inconsistent with the deed-based model but can be rationalized through the character-based model. As lined out in section 4, participants will react differently to information about the empirical reporting frequency depending on how they interpret it. Results from [Le Maux, Masclet, and Necker \(2021\)](#) show that participants respond to information even when their lies are perfectly observed and there thus is no credibility motive. They can be taken as further evidence that the credibility effect is not the only belief-based motive individuals hold. However, since this strand of experiments provides little experimental control over how participants update to information, it is difficult to imagine treatments in this framework that could falsify the character-based model.²⁹

[Bicchieri, Dimant, and Sonderegger \(2020\)](#) study the role of motivated beliefs in lying. They argue and provide consistent experimental evidence that individuals choose to believe that a higher fraction of other individuals are lying to justify their own lies. Thus, participants in their experiment choose to give up belief in the credibility of their report because the excuse that “everybody is doing it” or that “nobody is perfect” provides a better excuse for dishonesty.

²⁹An additional problem of experiments that provide the same information about past play to all participants is that underestimators might be different from overestimators in unobserved ways. In this case, the treatment assignment is not exogenous. This is not necessarily a problem if the goal of the treatment is to measure the average effect of information provision. However, it renders these experiments less informative about potential theoretical mechanisms.

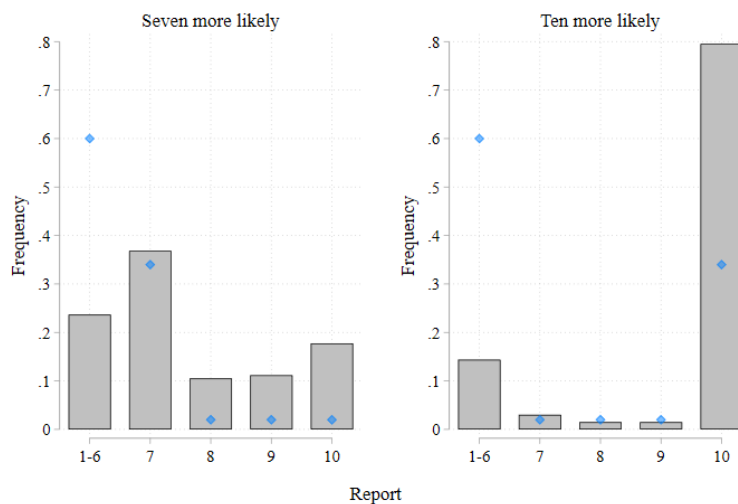
Bašić and Quercia (2022) show that participants who report higher payoffs in the die roll game are considered less trustworthy, which is reflected on multiple dimensions. When asked for their judgement, observers indicate that they would be less likely to lend money to participants who report high payoffs or to employ them. This is consistent with the idea that reports in the lying game are diagnostic about moral types.³⁰

In the Online Appendix to their paper, AN&R present data from an intriguing additional experiment on image concerns and lying. In this experiment, participants randomly draw one out of ten numbers and receive a higher payoff the higher the number they report. The distribution of the ten states is non-uniform and over two treatments, the authors vary whether the most likely state is either seven or ten, keeping the probability of drawing any of the other states constant. Figure 8 presents the report distribution observed in the experiment. The results indicate that participants who draw a number lower than seven become more likely to lie when probability mass is shifted from seven to ten. Furthermore, participants also tend to tell larger lies—partial lying is absent from the treatment where drawing ten is more likely than drawing seven.

Interestingly, the credibility and composition channels discussed in this paper might both contribute to the treatment difference observed by AN&R. The credibility channel will likely matter because, when the likelihood of drawing ten increases, reporting ten appears more credible and participants have smaller incentives to disguise their lie by lying partially. In addition, the increase in the probability of drawing ten comes at the expense of a decrease in the probability of drawing seven. Therefore, the composition of liars could also be affected by the treatment; participants might believe that liars are more likely to have drawn a number smaller than seven in the treatment where ten is more likely than in the treatment where seven is more likely. This in turn would increase the average moral type of liars and thus the perceived attractiveness of lying. Both channels predict the observed treatment effect and could thus jointly account for the observed data.

³⁰Bašić and Quercia (2022) further show that increasing the degree of observability in the game decreases lying. An additional intervention that increased self image concerns had no measurable effect on average reported die rolls.

Figure 8. Experimental data from AN&R's F10_LOW and F10_HIGH treatments



Note: The histogram shows the distribution of reports for two (between-subject) treatments conducted by AN&R, with a total of 284 participants. The blue dots illustrate the expected distribution of draws. The data used in this figure is available under <https://doi.org/10.3982/ECTA14673>.

7 Conclusion

The paper presented a model where agents derive reputational esteem from being perceived as an honest character. Such a model can explain many of the previous experimental results on lying games. Differences with other lying models emerge because agents' signaling motives differ (character vs. deed). The results are useful in applications to the behavioral effects of norm interventions or narratives, make predictions about the short- and long-term effects of different shaming conventions, and have implications on how lies should be disclosed.

Going ahead, I identify three types of possible future experimental research that could be informed by the theoretical lessons from this paper.

First, future experiments could address specific behavioral mechanisms identified by the theory and measure their empirical relevance. For example, to measure a preference for appearing honestly, researchers could elicit the willingness to pay for participating in a lying game. The character-based model would predict that participants are willing to pay a premium to not to participate in the lying game to signal their honesty. An alternative question regards the heterogeneity of the image concern. Since such heterogeneity leads to downward lying, trying to find ways to (non-deceptively)

study downward lying seems promising.³¹ One approach could try to create a situation where the experimenter knows the individual draw but where participants report to a person who does not know it (e.g. another participant in the experiment). The experimenter would thus be able to collect information on both individual draws and reports while still keeping signaling motives that might motivate some to lie downward active. Finding that participants in this setting lie downward would be a strong indicator of heterogeneous image concerns.

Second, future experiments could not only try to identify preferences but also the strategic reasoning of individuals that hold these preferences. In the current context, experiments that reinforce or create certain signaling motives through monetary incentives seem attractive. For example, introducing an investigator who might disclose and punish liars could serve to increase the credibility motive. Giving participants instrumental motives to appear trustworthy, e.g., by including a stage after the lying game in which participants play a trust game could increase participants' concern about the composition of types that their report pools them with.

Third, the paper's applications show that beliefs can influence lying behavior through numerous reasons. In the character-based model, in addition to the question on *how many* people lie, questions such as *who* lies and *why* become important. Designs which hold the objective statistical data provided to participants about reporting of others constant but change the interpretation of the data provided along with it (similarly to what [Hillenbrand and Verrina, 2022](#), do in the context of a dictator giving experiment) could test the behavioral relevance of narratives that aim to raise the credibility or composition signaling motive. Finally, besides the positive question of whether deed- or character-based signaling better explains behavior, there is also an additional normative question about whether one image concern leads to better outcomes than the other. The end of section 4.1 briefly touches upon this point in the context of potential dynamic effects when agents signal repeatedly. More detailed formal welfare comparisons would certainly be valuable.

³¹Experimental evidence on downwards lying so far has only been observed for selected samples and under special design features. In an experiment with a small sample of nuns, [Utikal and Fischbacher \(2013\)](#) find evidence that is consistent with downward lying. [Barron \(2019\)](#) finds systematic evidence that lab participants lie downwards on a small stakes die when they simultaneously have the opportunity to lie upwards on a high stakes die.

A Proofs

A.1 Proof of Proposition 1

(i) An agent who draws state j will lie if there is a state k such that

$$y(k) - t + \mu\mathcal{R}_k > y(j) + \mu\mathcal{R}_j. \quad (3)$$

Since $y(K) > y(j)$ for $j < K$, there cannot be an equilibrium where all agents tell the truth. In this case, the reputational payoff would not depend on the reported state, and there would be an agent of type (j, ϵ) , where $\epsilon > 0$ is arbitrarily close to zero, who could gain by reporting K . Because lying costs are fixed, agents always can make a report a to gain a gross payoff before lying costs of size $a \in \arg \max_{a \in \mathcal{K}} y(a) + \mu\mathcal{R}_a$. These considerations imply point (i).

(ii) It is useful to define a set

$$\mathcal{H} = \left\{ j \in \mathcal{K} \mid j \in \arg \max_{a \in \mathcal{K}} y(a) + \mu\mathcal{R}_a \right\}$$

that collects all states that are reported dishonestly with positive likelihood in equilibrium. If someone who draws j lies, this implies by utility maximization that $j \notin \mathcal{H}$. Therefore, no agent will lie and report j if $s(a \neq j \mid j, t) > 0$ for some type. By the same reasoning, no agent will lie if they draw a state $j \in \mathcal{H}$, as lying is costly and does not lead to higher payoffs.

(iii) Consider again the incentive constraint (3) and note that the payoff from lying strictly decreases in the lying cost. It follows that an agent lies if their lying cost is sufficiently low. In particular, for each state j there will be a threshold lying cost \hat{t}_j and agents (j, t) will lie if $t \leq \hat{t}_j$, where $\hat{t}_j > 0$ if $j \notin \mathcal{H}$ and $\hat{t}_j = 0$ otherwise. Now consider the reputations that are associated with agents who draw state j . Truth-tellers comprise the upper tail of the preference distribution, while liars make up the lower tail. Truth-tellers and liars have an expected cost of respectively

$$\begin{aligned} \mathcal{M}^+(\hat{t}_j) &\equiv \mathbb{E}(t \mid t > \hat{t}_j), \\ \mathcal{M}^-(\hat{t}_j) &\equiv \mathbb{E}(t \mid t \leq \hat{t}_j). \end{aligned}$$

Part (ii) implies that, if a state is not lied at, its reputation is equal to the expected type of agents who are above the threshold;

$$\mathcal{R}_j = \mathcal{M}^+(\hat{t}_j) \text{ if } j \notin \mathcal{H}. \quad (4)$$

Claim 1: $K \in \mathcal{H}$. Suppose the contrary, $K \notin \mathcal{H}$. Then, for all states $j \in \mathcal{H}$,

$$y(j) + \mu\mathcal{R}_j > y(K) + \mu\mathcal{R}_K, \text{ and } y(K) > y(j). \quad (5)$$

This in particular implies that $\mathcal{R}_j > \mathcal{R}_K$ for all $j \in \mathcal{H}$. From (4) it follows that $\mathcal{R}_K > \mathbb{E}(t)$ and more generally $\mathbb{E}(t|\text{report } j \notin \mathcal{H}) > \mathbb{E}(t)$. By the martingale property of beliefs, it then follows that $\mathbb{E}(t|\text{report } j \in \mathcal{H}) < \mathbb{E}(t)$, which requires that $\mathcal{R}_j < \mathbb{E}(t)$ for some $j \in \mathcal{H}$.³² Combining the inequalities, we arrive at $\mathcal{R}_K > \mathbb{E}(t) > \mathcal{R}_j$ for some $j \in \mathcal{H}$, which is a contradiction to (5).

Claim 2: $1 \notin \mathcal{H}$. Suppose the contrary, $1 \in \mathcal{H}$. Then, for all states $j \notin \mathcal{H}$,

$$y(j) + \mu\mathcal{R}_j < y(1) + \mu\mathcal{R}_1, \text{ and } y(1) < y(j). \quad (6)$$

This in particular implies that $\mathcal{R}_1 > \mathcal{R}_j$ for all $j \in \mathcal{H}$. Since \mathcal{R}_1 is a convex combination of the prior and the reputation of liars, the highest value \mathcal{R}_1 can obtain is smaller than $\max\{\mathbb{E}(t), \max\{\hat{t}\}\} < \mathbb{E}(t|t > \max\{\hat{t}\})$. Since $\mathcal{R}_j = \mathbb{E}(t|t > \max\{\hat{t}\})$ for some $j \in \mathcal{H}$, we arrive at a contradiction to (6).

(iv) Consider an equilibrium where \mathcal{H} is a singleton. It then holds that

$$y(K-1) + \mu\mathcal{R}_{K-1} < y(K) + \mu\mathcal{R}_K,$$

because every liar must prefer to report K over $K-1$. We can rearrange this inequality to

$$\mathcal{R}_{K-1} - \mathcal{R}_K \leq \frac{\Delta(K, K-1)}{\mu}. \quad (7)$$

Since $K-1 \notin \mathcal{H}$, it follows from (4) that $\mathcal{R}_{K-1} > \mathbb{E}(t)$. Furthermore, if \mathcal{H} is a singleton then by the martingale property of beliefs, $\mathcal{R}_K > \mathbb{E}(t)$. The left-hand side of (7) is strictly positive. Thus, there is a contradiction if $\frac{\Delta(K, K-1)}{\mu}$ is sufficiently small.

³²The martingale property states that a Bayesian observer never changes her prior on average. In the present context, $E[\mathbb{E}(t|a)] = \mathbb{E}(t)$.

A.2 Proof of Proposition 2

We first provide two lemmas before proceeding with the proof.

Lemma 1 (Properties of $\hat{t}_j(\varphi)$). *The derivative $\frac{\partial \hat{t}_j(\varphi)}{\partial \varphi} \in (0, 1)$ if $j \notin \mathcal{H}$ and μ is small enough. The derivative is increasing in μ .*

Proof. $\hat{t}_j(\varphi)$ is implicitly defined in

$$\hat{t}_j + \mu [\mathcal{M}^+(\hat{t}_j) - \varphi] - \Delta(K, j) = 0.$$

Implicitly differentiating the equation brings

$$\frac{\partial \hat{t}_j(\varphi)}{\partial \varphi} = \frac{\mu}{1 + \mu \mathcal{M}^{\prime+}(\hat{t}_j(\varphi))} \text{ if } j \leq k^*,$$

where $\mathcal{M}^+(t) > 0$. Therefore, the derivative is between 0 and 1 if μ is small (e.g. $\mu \leq 1$). It also gets clear from taking the cross-derivative with respect to μ that the derivative is increasing in μ . \square

Lemma 2 (Properties of $\mathcal{L}(\hat{\mathbf{t}}(\varphi))$). *$\mathcal{L}(\hat{\mathbf{t}}(\varphi))$ is (i) a continuous function in φ whenever some $\hat{t}_j > 0$ with (ii) $\frac{d\mathcal{L}}{d\varphi} < 1$ if μ is small enough. There exists (iii) an interval $(\varphi^{\min}, \mathbb{E}(t))$, where*

$$\varphi^{\min} = \begin{cases} \mathbb{E}(t) - \Delta(K, 1)/\mu & \mathbb{E}(t) > \Delta(K, 1)/\mu \\ \xi & \text{otherwise} \end{cases}$$

and $\xi = \mathcal{L}(\xi)$ is a fixed-point. For all φ on this interval, \mathcal{L} is continuous and $\mathcal{L}(\hat{\mathbf{t}}(\varphi)) < \varphi$.

Proof. (i) The functions $\hat{t}_j(\varphi)$ and $\mathcal{M}^-(t)$ are continuous functions. The threshold types $\hat{\mathbf{t}}$ can take on values between $[0, \bar{t}]$ and the c.d.f. $F(t)$ is continuous on $\hat{t} \in (0, \bar{t}]$. Since $F(0) = 0$ and $\lim_{t \rightarrow 0} F(t) = 0$, $F(t)$ is also continuous on $[0, \bar{t}]$. Taking products, sums, and (nonzero) quotients of continuous functions preserves continuity, which ensures that $\mathcal{L}(\hat{\mathbf{t}}(\varphi))$ varies continuously with φ , whenever some $\hat{t}_j > 0$, so that the quotient in $\mathcal{L}(\hat{\mathbf{t}}(\varphi))$ is nonzero.

(ii) Write the derivative as

$$\frac{d\mathcal{L}}{d\varphi} = \sum_{j \in \mathcal{K}} \frac{\partial \mathcal{L}}{\partial \hat{t}_j} \frac{\partial \hat{t}_j}{\partial \varphi}.$$

Lemma 1 shows that $\frac{\partial \hat{t}_j}{\partial \varphi}$ increases in μ . Therefore, there is a small enough μ so that $\frac{d\mathcal{L}}{d\varphi} < 1$. Appendix D shows that $\mu \leq 1$ is sufficient in case $f(t)$ is log-concave.

(iii) Proposition 1 shows that there is always lying from 1, which implies that, in equilibrium, $y(K) + \mu\varphi > y(1) + \mu\mathbb{E}(t)$ and therefore in any equilibrium $\varphi > \max\{0, \mathbb{E}(t) - \Delta(K, 1)/\mu\}$. If $\mathbb{E}(t) > \Delta(K, 1)/\mu$ then it follows that $\mathcal{L}(\hat{t}(\varphi^{\min} + \varepsilon)) < \varphi^{\min} + \varepsilon$ for an arbitrarily small $\varepsilon > 0$ (since $\hat{t}_1(\varphi^{\min}) = 0$). The assumptions on \bar{t} ensure that agents with the highest moral type never lie even if $\varphi = \mathbb{E}(t)$. Therefore, $\mathcal{L}(\hat{t}(\mathbb{E}(t))) < \mathbb{E}(t)$. Since $\frac{d\mathcal{L}}{d\varphi} < 1$, it follows that $\mathcal{L}(\hat{t}(\varphi)) < \varphi$ for all $\varphi \in (\mathbb{E}(t) - \Delta(K, 1)/\mu, \mathbb{E}(t))$. If $\mathbb{E}(t) \leq \Delta(K, 1)/\mu$ then $\mathcal{L}(\hat{t}(0)) > 0$, since $\hat{t}_1(0) > 0$. However, as $\mathcal{L}(\hat{t}(\mathbb{E}(t))) < \mathbb{E}(t)$ and $\frac{d\mathcal{L}}{d\varphi} < 1$ there exists a unique fixed-point $\xi > 0$ at which $\mathcal{L}(\hat{t}(\xi)) = \xi$. Therefore, $\mathcal{L}(\hat{t}(\varphi)) < \varphi$ for all $\varphi \in (\xi, \mathbb{E}(t))$. \square

Proof of Proposition 2. I omit the proofs for claims (i)–(iv) in the proposition and instead focus on the existence and uniqueness of equilibrium.

Claim 1: For every φ there exists a unique threshold value k^* which is the maximum integer $j \in \{1, \dots, K-1\}$ such that $y(K) + \mu\varphi \geq y(j) + \mu\mathbb{E}(t)$. Suppose by contradiction that there is a k^* for which $y(K) + \mu\varphi \leq y(k^*) + \mu\mathbb{E}(t)$. But then, individuals can profitably deviate and report k^* , as in such an equilibrium $\mathcal{R}_{k^*} > \mathbb{E}(t) > \varphi$, and hence

$$y(k^*) + \mu\mathcal{R}_{k^*} > y(K) + \mu\varphi.$$

This establishes that for any k^* , $y(K) + \mu\varphi \geq y(k^*) + \mu\mathbb{E}(t)$.

To see that k^* is the largest integer, consider a case where $k^* < k'$ and

$$y(K) + \mu\varphi \geq y(k') + \mu\mathbb{E}(t).$$

Since k' is now being lied at, $\mathcal{R}_{k'} < \mathbb{E}(t)$. The inequality is a contradiction to the condition that in any such equilibrium, $y(K) + \mu\varphi = y(k') + \mu\mathcal{R}_{k'}$.

Claim 2: For every $\varphi \in (\varphi^{\min}, \mathbb{E}(t))$, the fraction of agents who lie is a function $S(\varphi) = \frac{1}{K} \sum_{j \in \mathcal{K}} F(\hat{t}_j(\varphi))$. S is continuous with $S'(\varphi) > 0$. The first part follows because agents only lie if their moral type is smaller than the threshold $\hat{t}_j(\varphi)$. Therefore, the fraction of agents who are liars is given by S . Continuity of S follows because $\hat{t}_j(\varphi)$ varies continuously between 0 and \bar{t} on $\varphi \in (\varphi^{\min}, \mathbb{E}(t))$ and because $F(t)$ is continuous for $t \in [0, \bar{t}]$. Moreover, $F'(t) > 0$ and $\hat{t}'_j(\varphi) \geq 0$, with strict inequality if $\hat{t}_j(\varphi) > 0$. And since $\hat{t}_1(\varphi) > 0$ for all $\varphi \in (\varphi^{\min}, \mathbb{E}(t))$, $S'(\varphi) > 0$.

Claim 3: For every $\varphi \in (\varphi^{\min}, \mathbb{E}(t))$, $D(\varphi) = \frac{1}{K} \sum_{j=k^+1}^K \frac{1-r_j(\varphi)}{r_j(\varphi)}$ is continuous with $D'(\varphi) < 0$. In equilibrium, $D(\varphi) = P(\text{lie})$. The fraction of liars that report a state larger than k^* is*

$$\sum_{j=k^*+1}^K P(\text{report } j) \times P(\text{lie}|\text{report } j). \quad (8)$$

We defined $r_j = P(\text{truth}|\text{report } j)$. By Bayes' Rule,

$$r_j = \frac{P(\text{report } j \wedge \text{truth})}{P(\text{report } j)} \text{ for } j > k^*.$$

Observe that in equilibrium exactly $\frac{1}{K}$ agents report each state $j > k^*$ truthfully. Thus, we can rearrange the above equation to

$$P(\text{report } j) = \frac{1}{K} \frac{1}{r_j}.$$

Plugging into (8), we arrive at the following expression

$$\sum_{j=k^*+1}^K P(\text{report } j) \times P(\text{lie}|\text{report } j) = \frac{1}{K} \sum_{j=k^*+1}^K \frac{1-r_j}{r_j}. \quad (9)$$

We can derive an expression for r_j depending on φ by noting that,

$$\mathbb{E}(t|j) = r_j E(t) + (1-r_j) \mathcal{L}(\hat{t}(\varphi)) \text{ for all } j > k^*$$

and use the indifference condition from Proposition 1 (i) to replace $\mathbb{E}(t|j) = \varphi + \frac{\Delta(K,j)}{\mu}$ to derive

$$r_j(\varphi) = \frac{\varphi + \Delta(K,j)/\mu - \mathcal{L}(\hat{t}(\varphi))}{\mathbb{E}(t) - \mathcal{L}(\hat{t}(\varphi))}. \quad (10)$$

Finally, we define

$$D(\varphi) \equiv \frac{1}{K} \sum_{j=k^*+1}^K \frac{1-r_j(\varphi)}{r_j(\varphi)} = \frac{1}{K} \sum_{j=k^*+1}^K \frac{\mathbb{E}(t) - (\varphi + \Delta(K,j)/\mu)}{\varphi + \Delta(K,j)/\mu - \mathcal{L}(\hat{t}(\varphi))}. \quad (11)$$

The function $D(\varphi)$ is continuous as $\varphi > \mathcal{L}(\hat{t}(\varphi))$ for $\varphi \in (\varphi^{\min}, \mathbb{E}(t))$ and because the sum and quotient of continuous functions are continuous. $D(\varphi)$ is decreasing in φ : the

numerators in the sum term of (11) decrease in φ while the denominators increase as long as

$$\frac{d\mathcal{L}}{d\varphi} < 1,$$

which was shown in Lemma 2.

Claim 4: There exists a unique $\varphi^* \in (\varphi^{\min}, \mathbb{E}(t))$ such that $D(\varphi^*) = S(\varphi^*)$. From the previous claims, it follows that $D(\varphi)$ and $S(\varphi)$ are both continuous functions with $D'(\varphi) < 0$ and $S'(\varphi) > 0$. The intermediate value theorem guarantees a unique φ^* such that $D(\varphi^*) = S(\varphi^*)$. For existence of φ^* , observe that the parameter assumptions guarantee that $S(\varphi) \in (0, 1)$ for all $\varphi \in (\varphi^{\min}, \mathbb{E}(t))$. When $\varphi \rightarrow \varphi^{\min}$, $S(\varphi) = 0$ and $D(\varphi) > 0$. In the case where $\varphi \rightarrow \mathbb{E}(t)$, $k^* = K - 1$ and thus

$$\lim_{\varphi \rightarrow \mathbb{E}(t)} D(\varphi) = \lim_{\varphi \rightarrow \mathbb{E}(t)} \frac{1}{K} \frac{\mathbb{E}(t) - \varphi}{\varphi - \mathcal{L}(\hat{\mathbf{t}}(\varphi))} = 0.$$

It follows that

$$\lim_{\varphi \rightarrow \varphi^{\min}} [D(\varphi) - S(\varphi)] > 0, \text{ and } \lim_{\varphi \rightarrow \mathbb{E}(t)} [D(\varphi) - S(\varphi)] < 0.$$

As the difference is continuous and strictly decreasing there exists a unique $\varphi^* \in (\varphi^{\min}, \mathbb{E}(t))$ such that $D(\varphi^*) = S(\varphi^*)$. \square

A.3 Proof of Proposition 3a

The proof below makes use of properties of log-concave distribution functions. The following lemma states results for log-concave distribution functions that the proof will refer to.

Lemma 3. *Suppose density $f(t)$ is log-concave with $f(t) > 0$ for $t \in (0, \bar{t}]$.*

- (i) *The hazard rate $h(t) \equiv f(t)/(1 - F(t))$ increases in t and the inverse hazard rate $\iota(t) \equiv f(t)/F(t)$ decreases in t .*
- (ii) *$\mathcal{M}^{+'}(t) \in (0, 1)$ and $\mathcal{M}^{-'}(t) \in (0, 1)$.*
- (iii) *If f is strictly increasing, $\mathcal{M}^+(t) \leq 1/2 \leq \mathcal{M}^-(t)$ (for strictly decreasing f , $\mathcal{M}^+(t) \geq 1/2 \geq \mathcal{M}^-(t)$).*

Proof. Point (i) follows because if $f(t)$ is log concave then $F(t)$ and $1 - F(t)$ are also log concave and because $g'(t)/g(t)$ is decreasing for any log concave function $g(t)$ (see, e.g., [Bagnoli and Bergstrom, 2005](#)).

For proofs of points (ii) and (iii), see Lemma 1 in [Harbaugh and Rasmusen \(2018\)](#). □

Proof of Proposition 3a. Define $v(t) \equiv 1 - r(t)$ and $w(t) \equiv \mathcal{M}^+(t) - \mathcal{M}^-(t)$. We can rewrite

$$\Psi(t) = 2v(t)w(t).$$

The function $v(t)$ is increasing. [Jewitt \(2004\)](#) shows that if $f(t)$ is always decreasing $w(t)$ is always increasing, if $f(t)$ is always increasing $w(t)$ is always decreasing and if $f(t)$ is first increasing and then decreasing then $w(t)$ is first decreasing and then increasing. The claim of the proposition immediately follows for $f(t)$ decreasing. We further show the claim for log-concave distributions. Examine the logarithm of $\Psi(t)$. Its derivative with respect to t is

$$\frac{\partial \log(\Psi(t))}{\partial t} = \frac{1}{w(t)} \left[\frac{v'(t)}{v(t)} w(t) + w'(t) \right] = \frac{1}{w(t)} \left[\frac{f(t)}{F(t)(1+F(t))} (\mathcal{M}^+(t) - \mathcal{M}^-(t)) + \mathcal{M}^{+'}(t) - \mathcal{M}^{-'}(t) \right]. \quad (12)$$

The derivatives of the conditional expectation terms are

$$\mathcal{M}^{+'}(t) = h(t)(\mathcal{M}^+(t) - t),$$

$$\mathcal{M}^{-'}(t) = \iota(t)(t - \mathcal{M}^-(t)),$$

where $h(t)$ and $\iota(t)$ are as defined in Lemma 3. The derivative term (12) can only be nonpositive whenever the term in brackets is nonpositive. This condition can be rearranged to

$$\iota(t)(\mathcal{M}^+(t) - t) - \iota(t)(t - \mathcal{M}^-(t)) + 2\mathcal{M}^{+'}(t) \leq 0.$$

For this inequality to hold it is necessary that $t - \mathcal{M}^-(t) > \mathcal{M}^+(t) - t$. By part (ii) of Lemma 3, $t - \mathcal{M}^-(t)$ is increasing while $\mathcal{M}^+(t) - t$ is decreasing. Both terms cross once on $(0, \bar{t}]$. An additional necessary condition for $\Psi'(t) \leq 0$ is that $\mathcal{M}^{-'}(t) > \mathcal{M}^{+'}(t)$. Let \tilde{t} denote the median of $f(t)$ and consider the following two cases.

Case 1: $\tilde{t} \leq \mathbb{E}(t)$. By the martingale property of beliefs, $\mathcal{M}^+(t) + \mathcal{M}^-(t) = \frac{\mathbb{E}(t) - (1 - 2F(t))\mathcal{M}^+(t)}{F(t)}$. Plugging in \tilde{t} , from $F(\tilde{t}) = 1/2$ it follows that $\mathcal{M}^+(\tilde{t}) + \mathcal{M}^-(\tilde{t}) = 2E(t)$. Therefore, $\mathcal{M}^+(\tilde{t}) - \tilde{t} \geq \tilde{t} - \mathcal{M}^-(\tilde{t})$. At \tilde{t} , $h(\tilde{t}) = \iota(\tilde{t})$. Combined, these conditions imply that $\mathcal{M}^{+'}(\tilde{t}) \geq \mathcal{M}^{-'}(\tilde{t})$. Log-concavity implies that there is one \hat{t}' so that $\mathcal{M}^{-'}(t) > \mathcal{M}^{+'}(t)$ for $t < \hat{t}'$ and $\mathcal{M}^{-'}(t) \leq \mathcal{M}^{+'}(t)$ otherwise. There thus is no t for which both $t - \mathcal{M}^-(t) > \mathcal{M}^+(t) - t$ and $\mathcal{M}^{-'}(t) > \mathcal{M}^{+'}(t)$ hold. We conclude that $\Psi'(t) > 0$.

Case 2: $\tilde{t} > \mathbb{E}(t)$. Similar steps as above show that we cannot refute both necessary conditions when $\tilde{t} > \mathbb{E}(t)$, i.e., when $f(t)$ is left-skewed. We derive tighter conditions and show that the claim holds nonetheless in the case where f is always increasing (i.e., maximally left-skewed). Rearranging the bracket term in (12) and using $r(t) > 1/2$ for $t \in (0, \tilde{t})$, a necessary condition for $\Psi'(t) > 0$ is that

$$\frac{1}{F(t)}\mathcal{M}^{+'}(t) > \mathcal{M}^{-'}(t) - \mathcal{M}^{+'}(t). \quad (13)$$

This inequality holds as $t \rightarrow 0$; the l.h.s. goes to infinity and the r.h.s. is always smaller than one. Consider the derivative $\mathcal{M}^{+'}(t)$ as $t \rightarrow \tilde{t}$. Solving for the limit by repeatedly using l'hopital's rule:

$$\begin{aligned} \lim_{t \rightarrow \tilde{t}} \mathcal{M}^{+'}(t) &= \lim_{t \rightarrow \tilde{t}} \frac{f(t) \int_t^{\tilde{t}} (1 - F(s)) ds}{(1 - F(t))^2} \\ &= \lim_{t \rightarrow \tilde{t}} \frac{f'(t) \int_t^{\tilde{t}} (1 - F(s)) ds - f(t)(1 - F(t))}{-2f(t)(1 - F(t))} \\ &= \frac{1}{2} - \lim_{t \rightarrow \tilde{t}} \frac{f'(t) \int_t^{\tilde{t}} (1 - F(s)) ds}{2f(t)(1 - F(t))} \\ &= \frac{1}{2} - \lim_{t \rightarrow \tilde{t}} \frac{f''(t) \int_t^{\tilde{t}} (1 - F(s)) ds - f'(t)(1 - F(t))}{2f(t)(1 - F(t)) - 2f'(t)f(t)} = \frac{1}{2}. \end{aligned}$$

We use this result to show that inequality (13) holds as $t \rightarrow \tilde{t}$, as

$$\lim_{t \rightarrow \tilde{t}} \frac{1}{F(t)}\mathcal{M}^{+'}(t) = \frac{1}{2} > \lim_{t \rightarrow \tilde{t}} (\mathcal{M}^{-'}(t) - \mathcal{M}^{+'}(t)) = \underbrace{\mathcal{M}^{-'}(\tilde{t})}_{<1} - \frac{1}{2}.$$

Inequality (13) thus holds at the extreme points of t . Suppose that it does not hold for some intermediate values of t . In this case the l.h.s. would have to cut the r.h.s. at

least twice, once from above and once from below. We show in a last step that the l.h.s. can cross the r.h.s. only from above. Suppose there is a t' such that $\frac{1}{F(t')} \mathcal{M}^{+'}(t') = \mathcal{M}^{-'}(t') - \mathcal{M}^{+'}(t')$. If the l.h.s. cuts from above this means that the derivative of the l.h.s., evaluated at t' , is smaller than the derivative of the r.h.s. evaluated at t' . Expressed formally,

$$\frac{1}{F(t')} [\mathcal{M}^{+''}(t') - \iota(t') \mathcal{M}^{+'}(t')] < \mathcal{M}^{-''}(t') - \mathcal{M}^{+''}(t'). \quad (14)$$

The second derivatives of the conditional expectations are

$$\begin{aligned} \mathcal{M}^{+''}(t) &= \frac{f'(t)}{f(t)} \mathcal{M}^{+'}(t) + h(t)(2\mathcal{M}^{+'}(t) - 1), \\ \mathcal{M}^{-''}(t) &= \frac{f'(t)}{f(t)} \mathcal{M}^{-'}(t) + \iota(t)(1 - 2\mathcal{M}^{-'}(t)). \end{aligned}$$

Plugging them into inequality (14) and rearranging,

$$\begin{aligned} & \frac{f'(t)}{f(t)} \left[\frac{1}{F(t')} \mathcal{M}^{+'}(t') - (\mathcal{M}^{-'}(t') - \mathcal{M}^{+'}(t')) \right] < \\ & \iota(t')(1 - 2\mathcal{M}^{-'}(t')) + h(t')(1 - 2\mathcal{M}^{+'}(t')) - \left[2h(t') \frac{1}{F(t')} \mathcal{M}^{+'}(t') - h(t') - \iota(t') \frac{1}{F(t')} \mathcal{M}^{+'}(t') \right]. \end{aligned}$$

The bracket term of the l.h.s. evaluated at t' is zero. We can replace $\frac{1}{F(t')} \mathcal{M}^{+'}(t')$ by $\mathcal{M}^{-'}(t') - \mathcal{M}^{+'}(t')$ on the r.h.s. and rearrange it to get to

$$0 < \iota(t')(1 - \mathcal{M}^{-'}(t')) + h(t')(1 - 2\mathcal{M}^{+'}(t')) + (h(t') - \iota(t') \mathcal{M}^{+'}(t')).$$

The first and second terms are positive as $1 > \mathcal{M}^{-'}(t') \geq 1/2 > \mathcal{M}^{+'}(t')$ (part (iii) of Lemma 3). Using $\mathcal{M}^{+'}(t') = F(t')/(1 + F(t')) \times \mathcal{M}^{-'}(t')$, the last term is positive as

$$h(t') - \iota(t') \frac{F(t')}{1 + F(t')} \mathcal{M}^{-'}(t') = h(t') - \underbrace{\frac{f(t')}{1 + F(t')}}_{< h(t')} \underbrace{\mathcal{M}^{-'}(t')}_{< 1} > 0.$$

It follows that the l.h.s. of inequality (13) can cross the r.h.s. at most once. Since the inequality holds as $t \rightarrow 0$ and at \bar{t} we conclude that it also holds for all t on $(0, \bar{t})$. \square

A.4 Proof of Proposition 3b

With K states, the comparative statics depend on the sign of the derivative $d\varphi^*/d\hat{t}_k$. The derivative of φ^* with respect to other parameters will also be relevant for further comparative statics. I provide a general result on properties of the derivative of φ^* with respect to a generic parameter x that I will refer to in this and in further proofs.

Lemma 4 (Derivative of φ^*). *Consider an equilibrium reputation $\varphi^*(x)$, which depends on a parameter x and where an equilibrium obtains when*

$$h(\varphi, x) \equiv K \times (S(\varphi, x) - D(\varphi, x)) = 0,$$

with

$$S(\varphi, x) = \frac{1}{K} \sum_{j \in \mathcal{K}} F(\hat{t}_j(\varphi, x), x),$$

$$D(\varphi, x) = \frac{1}{K} \sum_{j \in \mathcal{H}} \frac{m(\varphi, x) - \Delta(K, j)/\mu}{n(\varphi, x) + \Delta(K, j)/\mu}$$

(e.g., $m(\varphi, x) \equiv \mathbb{E}(t) - \varphi$ and $n(\varphi, x) \equiv \varphi - \mathcal{L}(t(\varphi), x)$). The derivative of the equilibrium $\varphi^*(x)$ with respect to x is

$$\frac{d\varphi^*}{dx} = \frac{\beta \left[\frac{\partial \tilde{r}}{\partial x} (\mathbb{E}(t) - \mathcal{L}(\varphi, x)) + (\tilde{r} \xi \frac{\partial m}{\partial x} - (1 - \tilde{r}) \frac{\partial n}{\partial x}) \right]}{\partial h / \partial \varphi}.$$

where

$$\tilde{r}(t) \equiv \frac{1}{1 + \sum_{j \in \mathcal{K}} \alpha_j^{*2} \sum_{j \in \mathcal{K}} F(\hat{t}_j)} \text{ and } \xi \equiv \tilde{r}(\hat{t}^*) \sum_{j \in \mathcal{K}} \alpha_j^{*2} (K - k^*) + (1 - \tilde{r}(\hat{t}^*)).$$

The derivative $d\varphi^*/dx > 0$ if and only if $\frac{\partial \tilde{r}}{\partial x} (\mathbb{E}(t) - \mathcal{L}(\varphi, x)) + (\tilde{r} \xi \frac{\partial m}{\partial x} - (1 - \tilde{r}) \frac{\partial n}{\partial x}) > 0$.

Proof. See the Appendix E. □

Proof of Proposition 3b. Decisions are strategic substitutes if and only if

$$\frac{d\hat{t}_j}{d\hat{t}_k} = \frac{\partial \hat{t}_j}{\partial \varphi} \frac{d\varphi^*}{d\hat{t}_k} < 0.$$

Since $\frac{d\hat{t}_j}{d\varphi} \geq 0$, the inequality holds only if $\frac{d\varphi^*}{d\hat{t}_k} < 0$. Denote by $\hat{\mathbf{t}}_{j \neq k}$ the vector of all thresholds excluding \hat{t}_k . Defining $m(\varphi, \hat{\mathbf{t}}_k) \equiv \mathbb{E}(t) - \varphi$ and $n(\varphi, \hat{\mathbf{t}}_k) \equiv \varphi - \mathcal{L}(\mathbf{t}_{j \neq k}(\varphi), \hat{\mathbf{t}}_k)$, the conditions of Lemma 4 apply. Noting that $\frac{dm}{d\hat{t}_k} = 0$ and $\frac{dn}{d\hat{t}_k} = -\frac{\partial \mathcal{L}}{\partial \hat{t}_k}$, decisions are strategic substitutes if and only if

$$(1 - \tilde{r}(\mathbf{t}_{j \neq k}(\varphi^*), \hat{\mathbf{t}}_k)) \frac{\partial \mathcal{L}}{\partial \hat{t}_k} + \frac{\partial \tilde{r}}{\partial \hat{t}_k} (\mathbb{E}(t) - \mathcal{L}(\mathbf{t}_{j \neq k}(\varphi^*), \hat{\mathbf{t}}_k)) < 0.$$

□

A.5 Proof of Proposition 4a

We show that the derivative

$$\frac{\partial \Psi_{\bar{t}}(t)}{\partial \bar{t}} = \underbrace{r_{\bar{t}}(t) \left(\frac{\partial \mathcal{M}_{\bar{t}}^+(t)}{\partial \bar{t}} - \frac{\partial E_{\bar{t}}(t)}{\partial \bar{t}} \right)}_{=a} + \underbrace{(1 - r_{\bar{t}}(t)) \frac{\partial \mathcal{M}_{\bar{t}}^+(t)}{\partial \bar{t}} - \frac{\partial r_{\bar{t}}}{\partial \bar{t}} (E_{\bar{t}}(t) - \mathcal{M}_{\bar{t}}^-(t, \bar{t}))}_{=b}.$$

is positive. The \bar{t} subscript denotes the upper bound and we will use $F_{\bar{t}}(t) = F(t)/F(\bar{t})$. The upper tail expectation is $\mathcal{M}_{\bar{t}}^+(t) = \frac{F(\bar{t})}{F(\bar{t}) - F(t)} \int_t^{\bar{t}} t f(t) dt$, which has derivative

$$\frac{\partial \mathcal{M}_{\bar{t}}^+(t)}{\partial \bar{t}} = \frac{f(\bar{t})}{1 - F(t)} \left(\bar{t} - F(t) \mathcal{M}_{\bar{t}}^+(t) \right).$$

Evaluated at $t = 0$ gives $\frac{\partial E_{\bar{t}}(t)}{\partial \bar{t}} = \frac{f(\bar{t})}{1 - F(0)} \left(\bar{t} - F(0) \mathcal{M}_{\bar{t}}^+(t) \right) = f(\bar{t}) \bar{t}$. Plugging into a ,

$$a = \frac{r_{\bar{t}}(t) f(\bar{t}) F(t)}{1 - F(t)} \left(\bar{t} - \mathcal{M}_{\bar{t}}^+(t) \right) > 0 \text{ for } t \in (0, \bar{t}).$$

The derivative of $r_{\bar{t}}(t)$ with respect to \bar{t} is

$$\frac{\partial r_{\bar{t}}(t)}{\partial \bar{t}} = \frac{f(\bar{t})(F(\bar{t}) + F(t)) - f(\bar{t})F(\bar{t})}{(F(\bar{t}) + F(t))^2} = \frac{f(\bar{t})F(t)}{(F(\bar{t}) + F(t))^2} = f(\bar{t}) r_{\bar{t}}(t) (1 - r_{\bar{t}}(t)).$$

We can plug the derivative formulas into b to get

$$\begin{aligned}
b &= (1 - r_{\bar{t}}(t)) \left(\frac{f(\bar{t})}{1 - F(t)} \left(\bar{t} - F(t) \mathcal{M}_{\bar{t}}^+(t) \right) - f(\bar{t}) r_{\bar{t}}(t) (\mathbb{E}_{\bar{t}}(t) - \mathcal{M}_{\bar{t}}^-(t)) \right) \\
&= f(\bar{t}) (1 - r_{\bar{t}}(t)) \left(\frac{1}{1 - F(t)} \left(\bar{t} - F(t) \mathcal{M}_{\bar{t}}^+(t) \right) - r_{\bar{t}}(t) (\mathbb{E}_{\bar{t}}(t) - \mathcal{M}_{\bar{t}}^-(t)) \right) \\
&> f(\bar{t}) (1 - r_{\bar{t}}(t)) \left(\frac{1}{1 - F(t)} \left(\bar{t} - F(t) \mathcal{M}_{\bar{t}}^+(t) \right) - (\mathbb{E}_{\bar{t}}(t) - \mathcal{M}_{\bar{t}}^-(t)) \right) \\
&> f(\bar{t}) (1 - r_{\bar{t}}(t)) \left(\bar{t} - F(t) \mathcal{M}_{\bar{t}}^+(t) - (\mathbb{E}_{\bar{t}}(t) - \mathcal{M}_{\bar{t}}^-(t)) \right) \\
&= f(\bar{t}) (1 - r_{\bar{t}}(t)) \left(\bar{t} - F(t) \mathcal{M}_{\bar{t}}^-(t) - F(\bar{t}) \mathcal{M}_{\bar{t}}^+(t) + F(\bar{t}) \mathbb{E}_{\bar{t}}(t) - (\mathbb{E}_{\bar{t}}(t) - \mathcal{M}_{\bar{t}}^-(t)) \right) \\
&= f(\bar{t}) (1 - r_{\bar{t}}(t)) \left(F(\bar{t}) (\bar{t} - \mathcal{M}_{\bar{t}}^+(t)) + (1 - F(\bar{t})) (\bar{t} - \mathbb{E}_{\bar{t}}(t)) + (1 - F(t)) \mathcal{M}_{\bar{t}}^-(t) \right) > 0.
\end{aligned}$$

In the equation above, the second-last step makes use of the martingale property, by replacing $F(t) \mathcal{M}_{\bar{t}}^+(t) = F(t) \mathcal{M}_{\bar{t}}^-(t) + F(\bar{t}) (\mathcal{M}_{\bar{t}}^+(t) - \mathbb{E}_{\bar{t}}(t))$. Therefore, the whole derivative is positive. After a decrease in \bar{t} , the stigma function cuts the direct payoff at a larger t , i.e., \hat{t} increases.

A.6 Proof of Proposition 4b

Decompose the stigma function into two parts like in the proof of Proposition 3a;

$$\Psi_X(t) = v_X(t) w_X(t)$$

under $f_X(t)$ and analogously for $f_Y(t)$. We know that $v_Y(t) = v_X(t - a)$ and $w_Y(t) = w_X(t - a)$. Therefore, $\Psi_Y(t) = \Psi_X(t - a)$. Since $\Psi'_X(t), \Psi'_Y(t) > 0$ and $a > 0$, $\Psi_Y(t) < \Psi_X(t)$ for all $t \in (0, \bar{t} - a]$. This implies that $\Psi_Y(t)$ cuts the direct payoff at a larger t than $\Psi_X(t)$ and the result follows.

A.7 Proof of Proposition 4c

The proof relies on a Lemma on the properties of the Unimodal Likelihood Ratio.

Lemma 5 (Metzger and Rüschemdorf (1991), Theorems 2.3 and 2.3 (c)). *If $f_X(t)/f_Y(t)$ is unimodal with maximum at \tilde{t}_1 , then $F_X(t)/F_Y(t)$ is unimodal with maximum at $\tilde{t}_2 > \tilde{t}_1$ and $(1 - F_X(t))/(1 - F_Y(t))$ is unimodal with a maximum at $\tilde{t}_3 < \tilde{t}_1$.*

Proof of Proposition 4c

Claim 1: Consider the inverse hazard rates $\iota_X(t)$ and $\iota_Y(t)$. There is a $\bar{t} \in (0, \bar{t})$ such that $\iota_X(t) > \iota_Y(t)$ for $t < \bar{t}$ and $\iota_X(t) \leq \iota_Y(t)$ for $t \geq \bar{t}$. By Lemma 5, the ratio $F_X(t)/F_Y(t)$ will be unimodal (first increasing and then decreasing) on $(0, \bar{t}]$. This implies that the sign of $f_X(t)/F_X(t) - f_Y(t)/F_Y(t)$ changes once from positive to negative, which implies the claim.

Claim 2: Consider the hazard rates $h_X(t)$ and $h_Y(t)$. There is a $\bar{t} \in (0, \bar{t})$ such that $h_X(t) > h_Y(t)$ for $t < \bar{t}$ and $h_X(t) \leq h_Y(t)$ for $t \geq \bar{t}$. By Lemma 5, the ratio $(1 - F_X(t))/(1 - F_Y(t))$ will be unimodal (first increasing and then decreasing) on $(0, \bar{t}]$. This implies that the sign of $f_X(t)/(1 - F_X(t)) - f_Y(t)/(1 - F_Y(t))$ changes once from positive to negative, which implies the claim.

Claim 3: $\mathcal{M}_X^-(t) \geq \mathcal{M}_Y^-(t)$ for all $t \in (0, \bar{t}]$. At $t = \bar{t}$, since the means of $f_Y(t)$ and $f_X(t)$ coincide, $\mathcal{M}_Y^-(\bar{t}) = \mathbb{E}_Y(t) = \mathbb{E}_X(t) = \mathcal{M}_X^-(\bar{t})$. Also, as $t \rightarrow 0$, both $\mathcal{M}_X^-(t)$ and $\mathcal{M}_Y^-(t)$ go to zero. Consider

$$\mathcal{M}'_X(t) - \mathcal{M}'_Y(t) = \iota_X(t)(\mathcal{M}_X^-(t) - \mathcal{M}_Y^-(t)) + (t - \mathcal{M}_Y^-(t))(\iota_X(t) - \iota_Y(t)).$$

Evaluated at \bar{t} , $\mathcal{M}'_X(\bar{t}) - \mathcal{M}'_Y(\bar{t}) = (\bar{t} - \mathbb{E}_Y(t))(\iota_X(\bar{t}) - \iota_Y(\bar{t}))$. By Claim 1, it follows that $\mathcal{M}'_X(\bar{t}) - \mathcal{M}'_Y(\bar{t}) < 0$, i.e., $\mathcal{M}_Y^-(\bar{t})$ cuts $\mathcal{M}_X^-(\bar{t})$ from below. Consider gradually decreasing t , starting at \bar{t} . As long as $\mathcal{M}'_X(t) - \mathcal{M}'_Y(t) < 0$, it holds that $\mathcal{M}_X^-(t) - \mathcal{M}_Y^-(t) > 0$. Observe that $\mathcal{M}'_X(t) - \mathcal{M}'_Y(t)$ can only be zero if $\mathcal{M}_X^-(t) - \mathcal{M}_Y^-(t)$ and $\iota_X(t) - \iota_Y(t)$ have opposite signs. It follows that the largest value for t where $\mathcal{M}'_X(t) - \mathcal{M}'_Y(t)$ is zero is where $\iota_X(t) - \iota_Y(t) > 0$ and $\mathcal{M}_X^-(t) - \mathcal{M}_Y^-(t) < 0$. Since the difference $\iota_X(t) - \iota_Y(t)$ changes its sign only once from positive to negative for possible values of t and $\iota_X(\bar{t}) - \iota_Y(\bar{t}) < 0$ (Claim 1), this is also the unique point where $\mathcal{M}'_X(t) - \mathcal{M}'_Y(t)$ is zero. This shows that $\mathcal{M}_X^-(t) - \mathcal{M}_Y^-(t)$ is quasiconcave, which, taken together with the fact that $\mathcal{M}_X^-(t) - \mathcal{M}_Y^-(t)$ is zero as $t \rightarrow 0$ and $t = \bar{t}$, implies the initial claim.

Claim 4: $\mathcal{M}_X^+(t) \leq \mathcal{M}_Y^+(t)$ for all $t \in (0, \bar{t}]$. At $t = \bar{t}$, since the means of $f_Y(t)$ and $f_X(t)$ coincide, $\mathcal{M}_Y^+(\bar{t}) = \bar{t} - \mathbb{E}_Y(t) = \bar{t} - \mathbb{E}_X(t) = \mathcal{M}_X^+(\bar{t})$. Also, as $t \rightarrow 0$, both $\mathcal{M}_X^+(t)$ and $\mathcal{M}_Y^+(t)$ go to $\mathbb{E}_X(t) = \mathbb{E}_Y(t)$. Consider

$$\mathcal{M}'_Y(t) - \mathcal{M}'_X(t) = h_X(t)(\mathcal{M}_Y^+(t) - \mathcal{M}_X^+(t)) + (\mathcal{M}_Y^+(t) - t)(h_Y(t) - h_X(t)).$$

As $t \rightarrow 0$, $\mathcal{M}'_X(t) - \mathcal{M}'_Y(t) = \mathbb{E}_X(t)(h_Y(t) - h_X(t))$. By Claim 2, it follows that

$\mathcal{M}'_Y(t) - \mathcal{M}'_X(t) > 0$. Therefore, $\mathcal{M}'_Y(t) > \mathcal{M}'_X(t)$ for small t . Consider gradually increasing t starting from zero. As long as $\mathcal{M}'_Y(t) - \mathcal{M}'_X(t) > 0$, it holds that $\mathcal{M}^+_X(t) > \mathcal{M}^+_Y(t)$. Observe that $\mathcal{M}'_Y(t) - \mathcal{M}'_X(t)$ is only zero if $\mathcal{M}^+_Y(t) - \mathcal{M}^+_X(t)$ and $h_Y(t) - h_X(t)$ hold the opposite sign. The smallest value t where $\mathcal{M}'_Y(t) - \mathcal{M}'_X(t)$ can be zero is where $\mathcal{M}^+_Y(t) - \mathcal{M}^+_X(t) > 0$ and where $h_Y(t) - h_X(t) < 0$. Since the difference $h_Y(t) - h_X(t)$ changes its sign only once from positive to negative for possible values of t (Claim 2), this is also the unique point where $\mathcal{M}'_Y(t) - \mathcal{M}'_X(t)$ is zero. This shows that $\mathcal{M}^-_X(t) - \mathcal{M}^-_Y(t)$ is quasiconcave, which, taken together with the fact that $\mathcal{M}^-_X(t) - \mathcal{M}^-_Y(t)$ is zero as $t \rightarrow 0$ and $t = \bar{t}$, implies the initial claim.

Claim 5: $\Psi_Y(t) - \Psi_X(t) \geq 0$ for all $t \in (0, \bar{t}]$. As before, we use the definition

$$\Psi_Y(t) \equiv 2 \underbrace{v_Y(t)}_{\equiv \frac{F_Y(t)}{1+F_Y(t)}} \underbrace{w_Y(t)}_{\equiv \mathcal{M}^+_Y(t) - \mathcal{M}^-_Y(t)}$$

and symmetrically for $\Psi_X(t)$. The condition of the claim implies

$$\Psi_Y(t) - \Psi_X(t) \geq 0 \Rightarrow (v_Y(t) - v_X(t))w_X(t) + v_Y(t)(w_Y(t) - w_X(t)) \geq 0.$$

Consider that

$$v_Y(t) - v_X(t) = \frac{F_Y(t) - F_X(t)}{(1 + F_Y(t))(1 + F_X(t))}.$$

Plugging this into the initial condition and simplifying, we have

$$\begin{aligned} & \frac{F_Y(t) - F_X(t)}{1 + F_X(t)} w_X(t) + F_Y(t)(w_Y(t) - w_X(t)) \geq 0 \\ \Rightarrow & \frac{F_Y(t)}{1 + F_X(t)} w_X(t) - F_Y(t)w_X(t) + F_Y(t)w_Y(t) - \frac{F_X(t)}{1 + F_X(t)} w_X(t) \geq 0 \\ \Rightarrow & w_X(t) \left(\frac{F_Y(t)}{1 + F_X(t)} - F_Y(t) \right) + w_Y(t) \left(F_Y(t) - \frac{F_Y(t)}{1 + F_X(t)} \right) + \frac{F_Y(t)}{1 + F_X(t)} w_X(t) - \frac{F_X(t)}{1 + F_X(t)} w_X(t) \geq 0 \\ \Rightarrow & \left(F_Y(t) - \frac{F_Y(t)}{1 + F_X(t)} \right) (w_Y(t) - w_X(t)) + \frac{1}{1 + F_X(t)} (F_Y(t)w_Y(t) - F_X(t)w_X(t)) \geq 0. \end{aligned}$$

The first term is nonnegative as $F_Y(t) \geq F_Y(t)/(1 + F_X(t))$ and $w_Y(t) \geq w_X(t)$ by claims

3 and 4. By the martingale property of beliefs,

$$\mathbb{E}(t) = F(t)\mathcal{M}^-(t) + (1 - F(t))\mathcal{M}^+(t) \Rightarrow \mathcal{M}^+(t) - \mathcal{M}^-(t) = \frac{\mathcal{M}^+(t) - \mathbb{E}(t)}{F(t)}.$$

We can substitute this equality into the second term of the inequality above;

$$\frac{1}{1 + F_X(t)} (\mathcal{M}_Y^+(t) - \mathbb{E}_Y(t) - \mathcal{M}_X^+(t) + \mathbb{E}_X(t)).$$

It then follows from Claim 4 that this term is also nonnegative, with strict inequality for values on $(0, \bar{t})$. We conclude that the inequality holds for all possible t , which proves the claim.

The claims imply that $\Psi_Y(t) - \Psi_X(t) \geq 0$, with strict inequality for interior values of t . This implies that $\hat{t}_Y < \hat{t}_X$ when comparing two interior equilibria, which proves the proposition.

A.8 Proof of Proposition 4d

The equilibrium is characterized by a $\varphi^*(\theta)$ with equilibrium thresholds \hat{t}^* . We consider a marginal increase in θ . Lying from state \hat{t}_k decreases after an increase in θ if the threshold type \hat{t}_k decreases. This happens if

$$\frac{d\varphi^*}{d\theta} < \frac{\partial \mathcal{M}_\theta^+(\hat{t}_k^*)}{\partial \theta}. \quad (15)$$

Define $m(\varphi, \theta) \equiv E_\theta(t) - \varphi$ and $n(\varphi, \theta) = \varphi - \mathcal{L}_\theta(\hat{t}(\varphi, \theta))$, where the θ subscript denotes the dependence on θ through $f_\theta(t)$ and $F_\theta(t)$. By Lemma 4,

$$\frac{d\varphi^*}{d\theta} = \frac{\tilde{r}_\theta(\hat{t}^*)\xi \frac{\partial E_\theta(t)}{\partial \theta} + (1 - \tilde{r}_\theta(\hat{t}^*)) \frac{d\mathcal{L}_\theta}{d\theta} - \frac{d\tilde{r}_\theta}{d\theta} (E_\theta(t) - \mathcal{L}_\theta(\hat{t}^*))}{\frac{d\tilde{r}}{d\varphi^*} (E_\theta(t) - \mathcal{L}_\theta(\hat{t}^*)) + \tilde{r}_\theta(\hat{t}^*)\xi + (1 - \tilde{r}_\theta(\hat{t}^*)) (1 - \frac{\partial \mathcal{L}_\theta}{\partial \varphi^*})}.$$

Plugging the derivative term into (15) and rearranging gives

$$\begin{aligned} & \tilde{r}_\theta(\hat{t}^*)\xi \frac{\partial E_\theta(t)}{\partial \theta} + (1 - \tilde{r}_\theta(\hat{t}^*)) \frac{d\mathcal{L}_\theta}{d\theta} - \frac{d\tilde{r}_\theta}{d\theta} (E_\theta(t) - \mathcal{L}_\theta(\hat{t}^*)) < \\ & < \left[\frac{d\tilde{r}_\theta}{d\varphi} (E_\theta(t) - \mathcal{L}_\theta(\hat{t}^*)) + \tilde{r}_\theta(\hat{t}^*)\xi + (1 - \tilde{r}_\theta(\hat{t}^*)) (1 - \frac{\partial \mathcal{L}_\theta}{\partial \varphi}) \right] \frac{\partial \mathcal{M}_\theta^+(\hat{t}_k^*)}{\partial \theta}. \end{aligned}$$

We plug in $\frac{d\tilde{r}_\theta}{d\theta} = \frac{\partial\tilde{r}_\theta}{\partial\theta} + \sum_{j \in \mathcal{K}} \frac{\partial\tilde{r}_\theta}{\partial\hat{t}_j} \frac{\partial\hat{t}_j}{\partial\theta}$ and $\frac{d\mathcal{L}_\theta}{d\theta} = \frac{\partial\mathcal{L}_\theta}{\partial\theta} + \sum_{j \in \mathcal{K}} \frac{\partial\mathcal{L}_\theta}{\partial\hat{t}_j} \frac{\partial\hat{t}_j}{\partial\theta}$ to further rearrange to

$$\begin{aligned} & (\tilde{r}_\theta(\hat{\mathbf{t}}^*)\xi + (1 - \tilde{r}_\theta(\hat{\mathbf{t}}^*))) \frac{\partial\mathcal{M}_\theta^+(\hat{t}_k^*)}{\partial\theta} - \tilde{r}_\theta(\hat{\mathbf{t}}^*)\xi \frac{\partial E_\theta(t)}{\partial\theta} - (1 - \tilde{r}_\theta(\hat{\mathbf{t}}^*)) \frac{\partial\mathcal{L}_\theta}{\partial\theta} + \frac{\partial\tilde{r}_\theta}{\partial\theta} (E_\theta(t) - \mathcal{L}_\theta(\hat{\mathbf{t}}^*)) > \\ & (1 - \tilde{r}_\theta(\hat{\mathbf{t}}^*)) \sum_{j \in \mathcal{K}} \frac{\partial\mathcal{L}_\theta}{\partial\hat{t}_j} \frac{\partial\hat{t}_j}{\partial\theta} - \sum_{j \in \mathcal{K}} \frac{\partial\tilde{r}_\theta}{\partial\hat{t}_j} \frac{\partial\hat{t}_j}{\partial\theta} (\mathbb{E}(t) - \mathcal{L}_\theta(\hat{\mathbf{t}}^*)) + (1 - \tilde{r}_\theta(\hat{\mathbf{t}}^*)) \sum_{j \in \mathcal{K}} \frac{\partial\mathcal{L}_\theta}{\partial\hat{t}_j} \frac{\partial\hat{t}_j}{\partial\varphi} \\ & - \sum_{j \in \mathcal{K}} \frac{\partial\tilde{r}_\theta}{\partial\hat{t}_j} \frac{\partial\hat{t}_j}{\partial\varphi} (\mathbb{E}(t) - \mathcal{L}_\theta(\hat{\mathbf{t}}^*)) \frac{\partial\mathcal{M}_\theta^+(\hat{t}_k^*)}{\partial\theta}. \end{aligned}$$

Replacing $\frac{\partial\hat{t}_j}{\partial\theta} = -\frac{\partial\hat{t}_j}{\partial\varphi} \frac{\partial\mathcal{M}_\theta^+(\hat{t}_j^*)}{\partial\theta}$ and rearranging the r.h.s. gives the statement in the proposition.

A.9 Proof of Proposition 5a

With coarse disclosure, we have

$$\begin{aligned} r_j(\varphi) &= \frac{\varphi + \Delta(K, j)/\mu - \mathcal{L}(\hat{\mathbf{t}}(\varphi))}{(1 - \pi)(\mathbb{E}(t) - \mathcal{L}(\hat{\mathbf{t}}(\varphi)))}, \\ 1 - r_j(\varphi) &= \frac{(1 - \pi)\mathbb{E}(t) + \pi\mathcal{L}(\hat{\mathbf{t}}(\varphi)) - (\varphi + \Delta(K, j)/\mu)}{(1 - \pi)(\mathbb{E}(t) - \mathcal{L}(\hat{\mathbf{t}}(\varphi)))} \text{ for } j \in \mathcal{H}. \end{aligned}$$

Equilibrium is characterized by a function

$$h(\varphi, \pi) \equiv \frac{1}{K} \sum_{j \in \mathcal{K}} F(\hat{t}_j(\varphi)) - \frac{1}{K} \sum_{j \in \mathcal{H}} \frac{(1 - \pi)\mathbb{E}(t) + \pi\mathcal{L}(\hat{\mathbf{t}}(\varphi)) - (\varphi + \Delta(K, j)/\mu)}{\varphi + \Delta(K, j)/\mu - \mathcal{L}(\hat{\mathbf{t}}(\varphi))} = 0.$$

This function implicitly defines the equilibrium $\varphi^*(\pi)$. It increases in φ and in π . Consider two values π and $\pi' > \pi$. It holds that

$$h(\varphi^*(\pi'), \pi') = h(\varphi^*(\pi), \pi) = 0 < h(\varphi^*(\pi), \pi').$$

Therefore, $\varphi^*(\pi') < \varphi^*(\pi)$. Since $S'(\varphi) > 0$ lying is higher under π than under π' , which implies (ii).

To show point (i), that k^* weakly increases, consider that the proof of Proposition 2 shows that k^* is the largest state to which a liar would not deviate to. With an initial

probability of lie detection π , this condition becomes

$$y(K) + \mu\varphi^*(\pi) \geq y(k^*) + \mu[(1 - \pi)\mathbb{E}(t) + \pi\mathcal{L}(\hat{t}(\varphi^*(\pi)))].$$

After increasing π , the reputation terms of both the r.h.s. and the l.h.s. will adjust. If the decrease in reputation on the r.h.s. is larger than the decrease in reputation on the l.h.s., this inequality becomes more binding, which implies that it potentially will also hold for $k^* + 1$. If it holds for $k^* + 1$, the threshold state increases. We thus have to show that the difference

$$(1 - \pi)\mathbb{E}(t) + \pi\mathcal{L}(\hat{t}(\varphi^*(\pi))) - \varphi^*(\pi)$$

decreases in π . Plugging in, the difference becomes

$$(1 - r_K)(1 - \pi)[\mathbb{E}(t) - \mathcal{L}(\hat{t}(\varphi^*(\pi)))].$$

Taking the derivative with respect to π ;

$$-(1-r_K) \underbrace{(\mathbb{E}(t) - \mathcal{L}(\hat{t}(\varphi^*(\pi))))}_{>0} - \underbrace{\frac{\partial r_K}{\partial \pi}}_{>0} (1-\pi)(\mathbb{E}(t) - \mathcal{L}(\hat{t}(\varphi^*(\pi)))) + \underbrace{\frac{d\mathcal{L}}{d\pi}}_{<0} (1-r_K)(1-\pi) < 0.$$

Therefore, the threshold state weakly increases.

A.10 Proof of Proposition 5b

One issue with multiplicity arises as the equilibrium definition does not pin down the reputation of an agent from a state $j \in \mathcal{H}$ who (off equilibrium) is disclosed lying. A standard equilibrium refinement, which says that an off-equilibrium inference will attribute the message to the agent with the strongest incentive to deviate pins down off-equilibrium reputations after disclosure at $\mathcal{M}^-(0)$ and ensures uniqueness. Denote the investigator's policy by (π, γ) . The variable γ denotes the probability reveals a liar's drawn state. If $\gamma = 0$, we are under the coarse disclosure regime. Denote the part of state K 's reputation that is independent of $\mathcal{M}^-(\hat{t}_j)$ as

$$\varphi^C = (1 - \pi)[(r_K\mathbb{E}(t) + (1 - r_K)\mathcal{L}(\hat{t}))] + \pi(1 - \gamma)\mathcal{L}(\hat{t}).$$

A liar from a state j reporting K then has an expected reputation of $\varphi^C + \pi\gamma\mathcal{M}^-(\hat{t}_j)$. The threshold function becomes

$$\mathcal{T}(\Delta(K, j), \varphi^C, \pi, \gamma) \equiv t + \mu[R(t) - \varphi^C - \pi\gamma\mathcal{M}^-(t)] - \Delta(K, j) = 0,$$

so that the threshold $\hat{t}_j(\varphi^C, \pi, \gamma)$ now depends on π and γ . We denote the equilibrium threshold vector by $\hat{\mathbf{t}}^*$. Consider a marginal increase in γ . The thresholds change by

$$\frac{d\hat{t}_j}{d\gamma} = \frac{\partial\hat{t}_j}{\partial\varphi^C} \times \left(\frac{d\varphi^{C*}}{d\gamma} + \pi\mathcal{M}^-(\hat{t}_j^*) \right).$$

Under the uniform distribution, $\frac{\partial\hat{t}_j}{\partial\varphi^C} = \frac{\partial\hat{t}_k}{\partial\varphi^C} > 0$ for $j, k \leq k^*$ and zero otherwise. The aggregate lying rate is $\frac{1}{K} \frac{1}{i^*} \sum_{j \in \mathcal{K}} \hat{t}_j$, so that it decreases after a marginal increase in γ if

$$-k^* \frac{d\varphi^{C*}}{d\gamma} > \sum_{j \in \mathcal{K}} \pi\mathcal{M}^-(\hat{t}_j^*). \quad (16)$$

Using Lemma 4 (though note that, since $\pi > 0$, we have to adjust $\mathbb{E}(t) - \mathcal{L}(\hat{\mathbf{t}}^*)$ by $(1 - \pi)$), we find that

$$\frac{d\varphi^c}{d\gamma} = \frac{\left(\tilde{r}(\hat{\mathbf{t}}^*) \xi \frac{dm}{dx} - (1 - \tilde{r}(\hat{\mathbf{t}}^*)) \frac{dn}{dx} \right) - \frac{d\tilde{r}}{dx} (1 - \pi) (\mathbb{E}(t) - \mathcal{L}(\varphi, x))}{\frac{d\tilde{r}}{d\varphi} (1 - \pi) (\mathbb{E}(t) - \mathcal{L}(\hat{\mathbf{t}}^*)) + \tilde{r}(\hat{\mathbf{t}}^*) \xi + (1 - \tilde{r}(\hat{\mathbf{t}}^*)) (1 - \frac{d\mathcal{L}}{d\varphi})},$$

where $m(\varphi, \gamma) \equiv (1 - \pi)\mathbb{E}(t) + (1 - \pi\gamma)\mathcal{L}(\hat{\mathbf{t}}) - \varphi$ and $n(\varphi, \gamma) \equiv \varphi^C - (1 - \pi\gamma)\mathcal{L}(\hat{\mathbf{t}})$. Plugging this into (16) and rearranging gives

$$\begin{aligned} & ((1 - \tilde{r}(\hat{\mathbf{t}}^*)) + \xi\tilde{r}(\hat{\mathbf{t}}^*))k^* \left(\mathcal{L}(\hat{\mathbf{t}}^*) - \frac{1}{k^*} \sum_{j \in \mathcal{K}} \mathcal{M}^-(\hat{t}_j^*) \right) > \\ & > (1 - \pi) (\mathbb{E}(t) - \mathcal{L}(\hat{\mathbf{t}}^*)) \sum_{j \in \mathcal{K}} \frac{d\tilde{r}}{d\hat{t}_j} \frac{\partial\hat{t}_j}{\partial\varphi} \left(\sum_{k \in \mathcal{K}} \mathcal{M}^-(\hat{t}_k^*) - k^* \mathcal{M}^-(\hat{t}_j^*) \right) + \\ & + ((1 - \tilde{r}(\hat{\mathbf{t}}^*)) (1 - \pi\gamma) + \xi\tilde{r}(\hat{\mathbf{t}}^*) \pi (1 - \gamma)) \sum_{j \in \mathcal{K}} \left(\frac{\partial\mathcal{L}}{\partial\hat{t}_j} \frac{\partial\hat{t}_j}{\partial\varphi^C} (k^* \mathcal{M}^-(\hat{t}_j^*) - \sum_{k \in \mathcal{K}} \mathcal{M}^-(\hat{t}_k^*)) \right). \end{aligned}$$

The left hand side displays the direct effect of increasing γ , which is positive since there are relatively more large than small liars, implying that the weighted average of their

types is higher than the unweighted average; $\mathcal{L}(\hat{\mathbf{t}}(\varphi^C, \pi, \gamma)) > \frac{1}{k^*} \sum_{j \in \mathcal{K}} \mathcal{M}^-(\varphi^C, \pi, \gamma)$. The first term on the right hand side cancels out. To see this, note that $\frac{\partial \tilde{r}}{\partial \hat{t}_j} \frac{\partial \hat{t}_j}{\partial \varphi} = \frac{\partial \tilde{r}}{\partial \hat{t}_1} \frac{\partial \hat{t}_1}{\partial \varphi^C}$ for $j \leq k^*$ and zero otherwise, so that the derivative terms can be moved out of the sum and the remaining terms add up to zero. We move to the second term on the r.h.s. Rewrite

$$\begin{aligned}
\sum_{j \in \mathcal{K}} \left(\frac{\partial \mathcal{L}}{\partial \hat{t}_j} \frac{\partial \hat{t}_j}{\partial \varphi^C} (k^* \mathcal{M}^-(\hat{t}_j^*) - \sum_{k \in \mathcal{K}} \mathcal{M}(\hat{t}_k^*)) \right) &= \frac{\partial \hat{t}_1}{\partial \varphi^C} \left(k^* \sum_{j \in \mathcal{K}} \frac{\partial \mathcal{L}}{\partial \hat{t}_j} \mathcal{M}^-(\hat{t}_j^*) - \sum_{j \in \mathcal{K}} \frac{\partial \mathcal{L}}{\partial \hat{t}_j} \sum_{j \in \mathcal{K}} \mathcal{M}^-(\hat{t}_j^*) \right) \\
&= \frac{\partial \hat{t}_1}{\partial \varphi^C} \left(k^* \sum_{j \in \mathcal{K}} \frac{\hat{t}_j^* - \mathcal{L}(\hat{\mathbf{t}}^*)}{\sum_{l \in \mathcal{K}} \hat{t}_l} \frac{\hat{t}_j^*}{2} - \sum_{j \in \mathcal{K}} \frac{\hat{t}_j^* - \mathcal{L}(\hat{\mathbf{t}}^*)}{\sum_{l \in \mathcal{K}} \hat{t}_l} \sum_{j \in \mathcal{K}} \frac{\hat{t}_j^*}{2} \right) \\
&= \frac{\partial \hat{t}_1}{\partial \varphi^C} \frac{1}{\sum_{j \in \mathcal{K}} \hat{t}_j^*} \left(k^* \sum_{j \in \mathcal{K}} \left(\frac{\hat{t}_j^{*2}}{2} - \mathcal{L}(\hat{\mathbf{t}}^*) \frac{\hat{t}_j^*}{2} \right) - \left(\sum_{j \in \mathcal{K}} \hat{t}_j^* - k^* \mathcal{L}(\hat{\mathbf{t}}^*) \right) \sum_{j \in \mathcal{K}} \frac{\hat{t}_j^*}{2} \right) \\
&= \frac{\partial \hat{t}_1}{\partial \varphi^C} \frac{1}{\sum_{j \in \mathcal{K}} \hat{t}_j^*} \left(k^* \sum_{j \in \mathcal{K}} \frac{\hat{t}_j^{*2}}{2} - \sum_{j \in \mathcal{K}} \hat{t}_j^* \sum_{j \in \mathcal{K}} \frac{\hat{t}_j^*}{2} \right) \\
&= \frac{\partial \hat{t}_1^*}{\partial \varphi^C} k^* \left(\mathcal{L}(\hat{\mathbf{t}}^*) - \frac{1}{k^*} \sum_{j \in \mathcal{K}} \mathcal{M}^-(\hat{t}_j^*) \right).
\end{aligned}$$

Plugging the last two results into the inequality,

$$\begin{aligned}
&((1 - \tilde{r}(\hat{\mathbf{t}}^*)) + \xi \tilde{r}(\hat{\mathbf{t}}^*)) k^* \left(\mathcal{L}(\hat{\mathbf{t}}^*) - \frac{1}{k^*} \sum_{j \in \mathcal{K}} \mathcal{M}^-(\hat{t}_j^*) \right) > \\
&> ((1 - \tilde{r}(\hat{\mathbf{t}}^*))(1 - \pi\gamma) + \xi \tilde{r}(\hat{\mathbf{t}}^*) \pi(1 - \gamma)) \frac{\partial \hat{t}_1}{\partial \varphi^C} k^* \left(\mathcal{L}(\hat{\mathbf{t}}^*) - \frac{1}{k^*} \sum_{j \in \mathcal{K}} \mathcal{M}^-(\hat{t}_j^*) \right).
\end{aligned}$$

This inequality holds since $(1 - \tilde{r}(\hat{\mathbf{t}}^*)) + \xi \tilde{r}(\hat{\mathbf{t}}^*) \geq (1 - \tilde{r}(\hat{\mathbf{t}}^*))(1 - \pi\gamma) + \xi \tilde{r}(\hat{\mathbf{t}}^*) \pi(1 - \gamma)$ and $\frac{\partial \hat{t}_1}{\partial \varphi^C} < 1$ as long as μ is not too large. We conclude that the aggregate lying rate decreases. The average size of the lie increases because $\frac{d\hat{t}_1}{d\gamma} > \frac{d\hat{t}_j}{d\gamma} > 0 > \frac{d\hat{t}_{j+1}}{d\gamma} > \frac{d\hat{t}_{k^*}}{d\gamma}$ for some $j < k^*$, so that the proportion of lower states among liars increases, while the proportion of higher states decreases.

A.11 Proof of Proposition 6a

Suppose there is an equilibrium in which liars only report K . Then, there are $K - 1$ indifference conditions, which, for every state $1, \dots, K - 1$ determine a threshold type \hat{t}_j . Agents of type (j, t) will lie if $t \leq \hat{t}_j$. The indifference condition is

$$K + \mu\mathcal{R}_K - \hat{t}_j(K - j) = j + \mu\mathcal{R}_j,$$

which can be rewritten to

$$1 + \frac{\mu}{K - j}(\mathcal{R}_K - \mathcal{R}_j) = \hat{t}_j.$$

Note that in equilibrium $\mathcal{R}_K < \mathcal{R}_j$. It follows that $\hat{t}_1 > \dots > \hat{t}_{K-1}$. In equilibrium, no type can have an incentive to deviate and lie to a number different from K . Consider the type \hat{t}_1 . The incentive constraint postulates that

$$K + \mu\mathcal{R}_K - \hat{t}_1(K - 1) \geq K - 1 + \mu\mathcal{R}_{K-1} - \hat{t}_1(K - 2).$$

Rearranging, this condition is equal to

$$1 + \mu(\mathcal{R}_K - \mathcal{R}_{K-1}) \geq \hat{t}_1$$

Note however that in equilibrium,

$$1 + \mu(\mathcal{R}_K - \mathcal{R}_{K-1}) = \hat{t}_{K-1},$$

which implies $\hat{t}_1 \leq \hat{t}_{K-1}$, a contradiction. Therefore, an equilibrium where every liar reports K does not exist.

A.12 Proof of Proposition 6b

We construct the equilibrium stated in the proposition and then show that it exists. Denote by

$$\mathcal{M}^B(\hat{t}_a, \hat{t}_b) = \mathbb{E}(t | t \in (\hat{t}_a, \hat{t}_b])$$

the expected moral type if the moral type is between two thresholds $\hat{t}_a < \hat{t}_b$. Define a function

$$\mathcal{R}(\hat{t}_a, \hat{t}_b, j) \equiv \frac{(1 - F(\hat{t}_a))\mathcal{M}^+(\hat{t}_a) + (j - 1)(F(\hat{t}_b) - F(\hat{t}_a))\mathcal{M}^B(\hat{t}_a, \hat{t}_b)}{(1 - F(\hat{t}_a)) + (j - 1)(F(\hat{t}_b) - F(\hat{t}_a))}.$$

In the stated equilibrium, the reputations of the different states will be

$$\begin{aligned} \mathcal{R}_j(\hat{t}_j, \hat{t}_{j-1}) &= \mathcal{R}(\hat{t}_j, \hat{t}_{j-1}, j) \text{ if } j > 1 \text{ and} \\ \mathcal{R}_1(\hat{t}_1) &= \mathcal{M}^+(\hat{t}_1). \end{aligned}$$

The equilibrium \hat{t} -thresholds are determined by a number of indifference conditions. For example, the type \hat{t}_1 must be indifferent between truthfully reporting 1 or lying to report 2;

$$2 + \mu\mathcal{R}(\hat{t}_2, \hat{t}_1, 2) - \hat{t}_1 = 1 + \mu\mathcal{M}^+(\hat{t}_1).$$

Rearranging this condition, we can define a function $\mathcal{T}_1(\hat{t}_1, \hat{t}_2) \equiv 1 + \mu(\mathcal{R}(\hat{t}_2, \hat{t}_1, 2) - \mathcal{M}^+(\hat{t}_1)) - \hat{t}_1$. In equilibrium, $\mathcal{T}_1(\hat{t}_1^*, \hat{t}_2^*) = 0$. In a similar fashion, we can define the functions

$$\begin{aligned} \mathcal{T}_j(\hat{t}_{j-1}, \hat{t}_j, \hat{t}_{j+1}) &\equiv 1 + \mu(\mathcal{R}(\hat{t}_{j+1}, \hat{t}_j, j + 1) - \mathcal{R}(\hat{t}_j, \hat{t}_{j-1}, j)) - \hat{t}_j \text{ for } j \in \{2, \dots, K - 2\} \text{ and} \\ \mathcal{T}_{K-1}(\hat{t}_{K-2}, \hat{t}_{K-1}) &\equiv 1 + \mu(\mathcal{R}(0, \hat{t}_{K-1}, K) - \mathcal{R}(\hat{t}_{K-1}, \hat{t}_{K-2}, K - 1)). \end{aligned}$$

All of them need to equal zero in equilibrium. We can solve them recursively. Begin with $\mathcal{T}_1(\hat{t}_1, \hat{t}_2)$ and fix \hat{t}_2 at any value between 0 and 1. Note that $\mathcal{R}(\hat{t}_j, \hat{t}_j, j) = \mathcal{M}^+(\hat{t}_j)$ and

$$\mathcal{R}(\hat{t}_j, 1, j) = \frac{(1 - F(\hat{t}_j))\mathcal{M}^+(\hat{t}_j) + (j - 1)(F(1) - F(\hat{t}_j))\mathcal{M}^B(\hat{t}_j, 1)}{(1 - F(\hat{t}_j)) + (j - 1)(F(1) - F(\hat{t}_j))} < \mathcal{M}^+(\hat{t}_j) \leq \mathcal{M}^+(1).$$

Therefore,

$$\begin{aligned} \mathcal{T}_1(\hat{t}_2, \hat{t}_2) &= 1 + \mu(\mathcal{M}^+(\hat{t}_2) - \mathcal{M}^+(\hat{t}_2)) - \hat{t}_2 = 1 - \hat{t}_2 > 0 \text{ and} \\ \mathcal{T}_1(1, \hat{t}_2) &= 1 + \mu(\mathcal{R}(\hat{t}_2, 1, 2) - \mathcal{M}^+(1)) - 1 = \mu(\mathcal{R}(\hat{t}_2, 1, 2) - \mathcal{M}^+(1)) \leq 0. \end{aligned}$$

By the intermediate value theorem, there exists a \hat{t}_1 for any $\hat{t}_2 \in (0, 1]$ which solves \mathcal{T}_1 . We conclude that \mathcal{T}_1 implicitly defines a function $\hat{t}_1^*(\hat{t}_2)$ with the properties $\hat{t}_1^*(\hat{t}_2) > \hat{t}_2$ if $\hat{t}_2 < 1$ and $\hat{t}_1^*(1) = 1$.

We can use this implicitly defined function to replace \hat{t}_1 in equation \mathcal{T}_2 ;

$$\mathcal{T}_2(\hat{t}_1^*(\hat{t}_2), \hat{t}_2, \hat{t}_3) = 1 + \mu(\mathcal{R}(\hat{t}_3, \hat{t}_2, 3) - \mathcal{R}(\hat{t}_2, \hat{t}_1^*(\hat{t}_2), 2)) - \hat{t}_2.$$

Making use of former results, note that for any $\hat{t}_3 \in (0, 1]$,

$$\begin{aligned} \mathcal{T}_2(\hat{t}_1^*(\hat{t}_3), \hat{t}_3, \hat{t}_3) &= 1 + \mu(\mathcal{M}^+(\hat{t}_3) - \underbrace{\mathcal{R}(\hat{t}_1^*(\hat{t}_3), \hat{t}_3, 2)}_{< \mathcal{M}^+(\hat{t}_3)}) - \hat{t}_3 > 0 \text{ and} \\ \mathcal{T}_2(\hat{t}_1^*(1), 1, \hat{t}_3) &= 1 + \mu(\mathcal{R}(\hat{t}_3, 1, 3) - \mathcal{M}^+(1)) - 1 \leq 0. \end{aligned}$$

Therefore, for any $\hat{t}_3 \in (0, 1]$, a \hat{t}_2 exists. We conclude that \mathcal{T}_2 implicitly defines a function $\hat{t}_2^*(\hat{t}_3)$ with the properties $\hat{t}_2^*(\hat{t}_3) > \hat{t}_3$ if $\hat{t}_3 < 1$ and $\hat{t}_2^*(1) = 1$.

Similar steps show that functions $\hat{t}_j^*(\hat{t}_{j+1})$ with the properties $\hat{t}_j^*(\hat{t}_{j+1}) > \hat{t}_{j+1}$ if $\hat{t}_{j+1} < 1$ and $\hat{t}_j^*(1) = 1$ exist for all $j \in \{3, \dots, K-2\}$. In a last step, we plug the function $\hat{t}_{K-2}^*(\hat{t}_{K-1})$ into \mathcal{T}_{K-1} ;

$$\mathcal{T}_{K-1}(\hat{t}_{K-2}^*(\hat{t}_{K-1}), \hat{t}_{K-1}) \equiv 1 + \mu(\mathcal{R}(0, \hat{t}_{K-1}, K) - \mathcal{R}(\hat{t}_{K-1}, \hat{t}_{K-2}^*(\hat{t}_{K-1}), K-1)).$$

Now note that $\mathcal{R}(0, 0, K) = \mathbb{E}(t)$, $\mathcal{R}(0, \hat{t}_{K-2}^*(0), K-1) < \mathbb{E}(t)$, and $\mathcal{R}(0, 1, K) < \mathbb{E}(t)$. Therefore,

$$\mathcal{T}_{K-1}(\hat{t}_{K-2}^*(0), 0) = 1 + \mu(\mathbb{E}(t) - \mathcal{R}(0, \hat{t}_{K-2}^*(0), K-1)) - \hat{t}_3 > 0 \text{ and} \quad (17)$$

$$\mathcal{T}_{K-1}(\hat{t}_{K-2}^*(1), 1) = 1 + \mu(\mathcal{R}(0, 1, K) - \mathcal{M}^+(1)) - 1 < 0. \quad (18)$$

This shows that a \hat{t}_{K-1} exists for which $\mathcal{T}_{K-1}(\hat{t}_{K-2}^*(\hat{t}_{K-1}), \hat{t}_{K-1}) = 0$. The indifference conditions can thus be solved recursively: Find \hat{t}_{K-1}^* for which $\mathcal{T}_{K-1}(\hat{t}_{K-2}^*(\hat{t}_{K-1}), \hat{t}_{K-1}) = 0$, plug this into $\hat{t}_{K-2}^*(\hat{t}_{K-1})$ to obtain \hat{t}_{K-2}^* , and so forth to finally obtain $\hat{t}_1^*(\hat{t}_2^*)$. The resulting \hat{t}_j^* give the equilibrium vector of threshold types. To see that all of them are strictly smaller than one, note that a threshold \hat{t}_j can only be equal to 1 if \hat{t}_{j+1} is equal to 1. Since $\hat{t}_{K-1}^* < 1$ in equilibrium (by the strict inequality in Equation (17)), $\hat{t}_{K-2}^* < 1$ and therefore all remaining thresholds are also strictly smaller than 1.

A.13 Proof of proposition 7a

Suppose there is an equilibrium where liars only report K . Thus, agents must strictly prefer reporting K to reporting $K - 1$, conditional on lying. This implies an incentive constraint which is most binding for types with $\bar{\mu}$;

$$y(K) + \bar{\mu}\mathcal{R}_K \geq y(K - 1) + \bar{\mu}\mathcal{R}_{K-1}.$$

Rearrange this to

$$\frac{\Delta(K, K - 1)}{\bar{\mu}} \geq \mathcal{R}_{K-1} - \mathcal{R}_K.$$

Now, the equilibrium is such that all states smaller than K must have a reputation weakly larger than $\mathbb{E}(t)$, since agents reporting these states are in the right tail of the moral type distribution. By the martingale property of beliefs we know that, conversely, $\mathcal{R}_K < \mathbb{E}(t)$. Therefore, the right-hand side of the inequality above is strictly positive. There is a contradiction if $\bar{\mu}$ is sufficiently large.

A.14 Proof of proposition 7b

In equilibrium, the moral type threshold of liars lying to K is given by

$$\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_j, \mu) \equiv \Delta(K, j) + \mu(\mathcal{R}_K - \mathcal{R}_j).$$

Similarly, the threshold of lying to $K - 1$ is equal to

$$\hat{t}_{K-1,j}(\mathcal{R}_K, \mathcal{R}_j, \mu) \equiv \Delta(K - 1, j) + \mu(\mathcal{R}_{K-1} - \mathcal{R}_j).$$

Liars prefer reporting K over reporting $K - 1$ if

$$y(K) + \mu\mathcal{R}_K \geq y(K - 1) + \mu\mathcal{R}_{K-1}.$$

From this, we can derive the threshold image type $\hat{\mu}$ who is indifferent between reporting K or $K - 1$;

$$\hat{\mu} = \frac{\Delta(K, K - 1)}{\mathcal{R}_{K-1} - \mathcal{R}_K}. \quad (19)$$

The reputation of state j in equilibrium is then given by

$$\mathcal{R}_j = \mathcal{R}(\mathcal{R}_K, \mathcal{R}_{K-1}, \mathcal{R}_j, \hat{\mu}, j) \equiv \frac{\int_0^{\hat{\mu}} \bar{F}(\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_j, \mu)) \mathcal{M}^+(\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_j, \mu)) g(\mu) d\mu + \int_{\hat{\mu}}^{\bar{\mu}} \bar{F}(\hat{t}_{K-1,j}(\mathcal{R}_{K-1}, \mathcal{R}_j, \mu)) \mathcal{M}^+(\hat{t}_{K-1,j}(\mathcal{R}_{K-1}, \mathcal{R}_j, \mu)) g(\mu) d\mu}{\int_0^{\hat{\mu}} \bar{F}(\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_j, \mu)) g(\mu) d\mu + \int_{\hat{\mu}}^{\bar{\mu}} \bar{F}(\hat{t}_{K-1,j}(\mathcal{R}_{K-1}, \mathcal{R}_j, \mu)) g(\mu) d\mu}$$

Define a function

$$\rho_j(\mathcal{R}_K, \mathcal{R}_{K-1}, \mathcal{R}_j, \hat{\mu}) \equiv \mathcal{R}(\mathcal{R}_K, \mathcal{R}_{K-1}, \mathcal{R}_j, \hat{\mu}, j) - \mathcal{R}_j.$$

In equilibrium $\rho_j(\mathcal{R}_K, \mathcal{R}_{K-1}, \mathcal{R}_j, \hat{\mu}) = 0$. Note that $\rho_j(\mathcal{R}_K, \mathcal{R}_{K-1}, \mathbb{E}(t), \hat{\mu}) = \mathcal{R}(\mathcal{R}_K, \mathcal{R}_{K-1}, \mathbb{E}(t), \hat{\mu}, j) - \mathbb{E}(t) > 0$ and that $\rho_j(\mathcal{R}_K, \mathcal{R}_{K-1}, \hat{\mu}, \bar{t}) = \mathcal{R}(\mathcal{R}_K, \mathcal{R}_{K-1}, \hat{\mu}, \bar{t}, j) - \bar{t} < 0$. Therefore, for any three parameters $\mathcal{R}_K, \mathcal{R}_{K-1}, \hat{\mu}$, we can always find a vector of equilibrium reputations $\mathcal{R}_1^*, \dots, \mathcal{R}_{K-2}^*$ of the lower states consistent with it.

The equilibrium reputation of $K - 1$ is equal to

$$\begin{aligned} \mathcal{R}_{K-1} = \mathcal{R}(\mathcal{R}_K, \mathcal{R}_{K-1}, \mathcal{R}_{K-2}, \dots, \mathcal{R}_1, \hat{\mu}) \equiv & \\ & \frac{1}{\int_0^{\hat{\mu}} \bar{F}(\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_j, \mu)) g(\mu) d\mu + \sum_{j \neq K-1} \int_{\hat{\mu}}^{\bar{\mu}} F(\hat{t}_{K-1,j}(\mathcal{R}_{K-1}, \mathcal{R}_j, \mu)) g(\mu) d\mu} \times \\ & \left[\int_0^{\hat{\mu}} \bar{F}(\hat{t}_{K,K-1}(\mathcal{R}_K, \mathcal{R}_{K-1}, \mu)) \mathcal{M}^+(\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_{K-1}, \mu)) g(\mu) d\mu + \right. \\ & \left. \sum_{j \neq K-1} \int_{\hat{\mu}}^{\bar{\mu}} F(\hat{t}_{K-1,j}(\mathcal{R}_{K-1}, \mathcal{R}_j, \mu)) \mathcal{M}^-(\hat{t}_{K-1,j}(\mathcal{R}_{K-1}, \mathcal{R}_j, \mu)) g(\mu) d\mu \right]. \end{aligned}$$

Note from Equation (19) that we can write the equilibrium $\hat{\mu}^*$ as a function of \mathcal{R}_K and \mathcal{R}_{K-1} . Replacing $\hat{\mu}$ and the lower reputations yields

$$\begin{aligned} \rho_{K-1}(\mathcal{R}_K, \mathcal{R}_{K-1}) \equiv & \\ & \mathcal{R}(\mathcal{R}_K, \mathcal{R}_{K-1}, \mathcal{R}_{K-2}^*(\mathcal{R}_K, \mathcal{R}_{K-1}, \hat{\mu}^*(\mathcal{R}_K, \mathcal{R}_{K-1})), \dots, \mathcal{R}_1^*(\mathcal{R}_K, \mathcal{R}_{K-1}, \hat{\mu}^*(\mathcal{R}_K, \mathcal{R}_{K-1})), \hat{\mu}^*(\mathcal{R}_K, \mathcal{R}_{K-1})) - \mathcal{R}_{K-1}. \end{aligned}$$

In equilibrium $\rho_j(\mathcal{R}_K, \mathcal{R}_{K-1}) = 0$. Fix \mathcal{R}_K at a value between 0 and $\mathbb{E}(t)$. Values that \mathcal{R}_{K-1} can take on that are compatible with equilibrium are on $[\mathcal{R}_K + \Delta(K, K - 1)/\bar{\mu}, \bar{t}]$.

Evaluating ρ_{K-1} at these extreme values;

$$\rho_{K-1}(\mathcal{R}_K, \bar{t}) = \mathcal{R}(\mathcal{R}_K, \bar{t}, \mathcal{R}_{K-2}^*(\mathcal{R}_K, \bar{t}, \hat{\mu}^*(\mathcal{R}_K, \bar{t})), \dots, \mathcal{R}_1^*(\mathcal{R}_K, \bar{t}, \hat{\mu}^*(\mathcal{R}_K, \bar{t})), \hat{\mu}^*(\mathcal{R}_K, \bar{t})) - \bar{t} < 0,$$

$$\rho_{K-1}(\mathcal{R}_K, \mathcal{R}_K + \Delta(K, K-1)/\bar{\mu}) = \frac{\int_0^{\hat{\mu}} \bar{F}(\hat{t}_{K,K-1}(\mathcal{R}_K, \mathcal{R}_{K-1}, \mu) \mathcal{M}^+(\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_{K-1}, \mu)) g(\mu) d\mu}{\int_0^{\hat{\mu}} \bar{F}(\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_j, \mu) g(\mu) d\mu} -$$

$$\left(\mathcal{R}_K + \frac{\Delta(K, K-1)}{\bar{\mu}} \right).$$

Since the first term on the r.h.s. in the equation above is always larger than $\mathbb{E}(t)$ and $\mathcal{R}_K < \mathbb{E}(t)$ in equilibrium, the r.h.s. is larger than zero as long as $\Delta(K, K-1)/\bar{\mu}$ is not too large. In this case, a solution exists such that $\rho_{K-1}(\mathcal{R}_K, \mathcal{R}_{K-1}^*(\mathcal{R}_K)) = 0$. Therefore, \mathcal{R}_K pins down all remaining reputations $\mathcal{R}_{K-1}, \dots, \mathcal{R}_1$ and also $\hat{\mu}$.

Lastly, we have to find a \mathcal{R}_K^* so that $\rho_K(\mathcal{R}_K^*) = 0$, where

$$\rho_K(\mathcal{R}_K) \equiv$$

$$\frac{1}{\int_{\hat{\mu}^*}^{\bar{\mu}} \bar{F}(\hat{t}_{K-1,K}(\mathcal{R}_{K-1}^*, \mathcal{R}_K, \mu) g(\mu) d\mu + \int_0^{\hat{\mu}^*} F(\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_j^*, \mu)) g(\mu) d\mu} \times$$

$$\left[\int_{\hat{\mu}}^{\bar{\mu}^*} \bar{F}(\hat{t}_{K-1,K}(\mathcal{R}_{K-1}^*, \mathcal{R}_K, \mu) \mathcal{M}^+(\hat{t}_{K-1,K}(\mathcal{R}_{K-1}^*, \mathcal{R}_K, \mu)) g(\mu) d\mu + \right.$$

$$\left. \sum_{j \neq K} \int_{\hat{\mu}^*}^{\bar{\mu}} F(\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_j^*, \mu)) \mathcal{M}^-(\hat{t}_{K,j}(\mathcal{R}_K, \mathcal{R}_j^*, \mu)) g(\mu) d\mu \right] - \mathcal{R}_K.$$

Since this function is strictly larger than zero when evaluated at 0 and strictly smaller than $\mathbb{E}(t)$ when evaluated at $\mathbb{E}(t)$, a solution exists.

B Example of a non-symmetric equilibrium

This section provides an example of an equilibrium where the reports of liars depends on their lying cost. Consider a setup with $K = 3$ and the following strategy profile:

$$\begin{aligned} s(j|j, t) &= 1 \text{ if } j > 1, \\ s(3|1, t) &= 1 \text{ if } t \leq \hat{t}_a \\ s(2|1, t) &= 1 \text{ if } t \in (\hat{t}_a, \hat{t}_b] \\ s(1|1, t) &= 1 \text{ if } t \geq \hat{t}_b. \end{aligned}$$

That is, agents lie only if they draw 1. There are two quality segments of liars. Liars with the worst quality report the highest state and other liars report the middle state.

Assume preferences are uniformly distributed between zero and $T > 0$. The equilibrium reputations are

$$\begin{aligned} \mathcal{R}_1(T, \hat{t}_b) &= \frac{T + \hat{t}_b}{2} \\ \mathcal{R}_2(T, \hat{t}_a, \hat{t}_b) &= \frac{1}{2} \times \frac{T^2 + (\hat{t}_a + \hat{t}_b)(\hat{t}_b - \hat{t}_a)}{T + \hat{t}_b - \hat{t}_a} \\ \mathcal{R}_3(T, \hat{t}_a) &= \frac{1}{2} \times \frac{T^2 + \hat{t}_a^2}{T + \hat{t}_a}. \end{aligned}$$

The equilibrium is characterized by two threshold values (\hat{t}_a, \hat{t}_b) and two indifference conditions. The first is that the agent of type $(1, \hat{t}_b)$ must be indifferent between lying and truth-telling;

$$\begin{aligned} y(1) + \mu \mathcal{R}_1(T, \hat{t}_b) &= y(3) + \mu \mathcal{R}_3(T, \hat{t}_a) - \hat{t}_b \\ \Rightarrow \hat{t}_b &= \frac{1}{1 + \mu/2} (\Delta(3, 1) + \mu(\mathcal{R}_3(T, \hat{t}_a) - T)). \end{aligned} \tag{20}$$

The second equilibrium condition is that liars must be indifferent between reporting states 2 and 3;

$$y(3) + \mu \mathcal{R}_3(T, \hat{t}_a) = y(2) + \mu \mathcal{R}_2(T, \hat{t}_a, \hat{t}_b). \tag{21}$$

Consider parameter values $\mu = 1$, $T = 7$, $y(1) = 0$, $y(2) = 4.9$, and $y(3) = 5$. We can plug Equation (20) into Equation (21) and solve for \hat{t}_a . The resulting parameter values

are $\hat{t}_a \approx 1.12$ and $\hat{t}_b \approx 3.06$, which imply that each of the states are reported (from low to high) with frequencies 18.75%, 42.57%, and 38.68%. Note that in this example, the second-highest state is reported with a higher frequency than the highest state. In the symmetric equilibrium with homogeneous image concerns the reporting frequencies are monotonely increasing in j . Therefore, the example induces a different reporting frequency than the one induced by symmetric equilibrium.

C Heterogenous image concerns

To illustrate the new features that can arise in an equilibrium with heterogenous image concerns, we will consider an example of a simple die roll game with only three different payoff levels, where reporting any number lower than five pays one, and reporting five or six pays five and six, respectively. We also keep heterogeneity in the image concern as simple as possible, by assuming that l -type agents are *homines oeconomici* with $\mu_l = 0$, who do not incur a moral cost from lying.³³

Example (Non-modality of the highest state) *Consider the simple die roll game as described above where h -types have $\mu_h = 3/2$ and draw their lying cost from a discrete distribution $(p : \underline{t}; (1 - p) : \bar{t})$, where $p = .5$ and $\bar{t} = 3.5 > \underline{t} = 3$. If $\rho = .21$, there is an equilibrium with no downwards lying and where more agents report five than six.*

Proof. The equilibrium described above is consistent with the following reputations;

$$\mathcal{R}_1 = \bar{t}, \mathcal{R}_5 = \frac{5p\underline{t} + (1 - p)\bar{t}}{1 + 4p}, \mathcal{R}_6 = \frac{(1 - \rho)(p\underline{t} + (1 - p)\bar{t})}{1 + 5\rho},$$

which imply the incentive constraints

$y(5) + \mu\mathcal{R}_5 - \underline{t} > y(1) + \mu\mathcal{R}_1$ (h -type agents with low lying costs prefer lying to 5 over honestly reporting 1)

$y(5) + \mu\mathcal{R}_5 - \bar{t} < y(1) + \mu\mathcal{R}_1$ (h -type agents with high lying costs prefer honestly reporting 1 over lying to 5)

$y(6) + \mu\mathcal{R}_5 = y(6) + \mu\mathcal{R}_6$ (h -type agents are indifferent between reporting 5 or 6)

By plugging in the parameter values, it can be verified that they indeed hold. In equi-

³³This approach follows [Grossman and van der Weele \(2017\)](#), who study the impact of introducing the homo oeconomicus on prosocial behavior in a character-based image model.

librium, the fraction of agents reporting six is

$$(1 - \rho)/6 + \rho \approx .34$$

and the fraction of agents reporting five is

$$(1 - \rho)/6 + (1 - \rho)p \times (4/6) \approx .40.$$

Therefore, more agents report five than six. □

This example shows that, with heterogenous image concerns, the partial lying motive can lead more agents to report the second highest state over the highest state. This is a consequence of the quality signaling motive. Among the different quality “segments” of liars, the *homines oeconomici* have the worst reputation. Image concerned agents might then be induced to report a state different from the highest state because they do not want to be mistaken for a *homo oeconomicus*, even if doing so is more obviously a lie.

D Remark: Upper bound on μ

The precise upper bound on μ will depend on the distribution function $F(t)$. Here we show that, if $F(t)$ is log-concave, $\frac{d\hat{t}_j}{d\varphi} < 1$ is sufficient (and therefore, e.g., $\mu \leq 1$ by Lemma 1). Suppose that this condition holds. A sufficient condition for $\frac{d\mathcal{L}}{d\varphi} < 1$ is that

$$\sum_{j \in \mathcal{K}} \frac{d\mathcal{L}}{d\hat{t}_j} \leq 1. \tag{22}$$

Taking derivatives, the sum term becomes

$$\begin{aligned}
\sum_{j \in \mathcal{K}} \frac{d\mathcal{L}}{d\hat{t}_j} &= \frac{\sum_{j \in \mathcal{K}}}{(\sum_{l \in \mathcal{K}} F(\hat{t}_l))^2} \left[f(\hat{t}_j) \mathcal{M}^-(\hat{t}_j) \sum_{l \in \mathcal{K}} F(\hat{t}_l) + F(\hat{t}_j) \mathcal{M}'(\hat{t}_j) \sum_{l \in \mathcal{K}} F(\hat{t}_l) - f(\hat{t}_j) \sum_{l \in \mathcal{K}} F(\hat{t}_l) \mathcal{M}^-(\hat{t}_l) \right] \\
&= \frac{\sum_{j \in \mathcal{K}}}{\sum_{l \in \mathcal{K}} F(\hat{t}_l)} [f(\hat{t}_j) \mathcal{M}^-(\hat{t}_j) + F(\hat{t}_j) \mathcal{M}'(\hat{t}_j) - f(\hat{t}_j) \mathcal{L}(\hat{\mathbf{t}}(\varphi))] \\
&= \frac{\sum_{j \in \mathcal{K}}}{\sum_{l \in \mathcal{K}} F(\hat{t}_l)} \left[f(\hat{t}_j) \mathcal{M}^-(\hat{t}_j) + F(\hat{t}_j) \frac{f(\hat{t}_j)}{F(\hat{t}_j)} (\hat{t}_j - \mathcal{M}^-(\hat{t}_j)) - f(\hat{t}_j) \mathcal{L}(\hat{\mathbf{t}}(\varphi)) \right] \\
&= \frac{\sum_{j \in \mathcal{K}} f(\hat{t}_j)}{\sum_{l \in \mathcal{K}} F(\hat{t}_l)} [\hat{t}_j - \mathcal{L}(\hat{\mathbf{t}}(\varphi))].
\end{aligned}$$

We now show that condition (22) always holds if $F(t)$ is log-concave. By log-concavity of $f(t)$, $\mathcal{M}'(t) \in (0, 1)$. It follows that

$$\sum_{j \in \mathcal{K}} \frac{F(\hat{t}_j)}{\sum_{l \in \mathcal{K}} F(\hat{t}_l)} \mathcal{M}'(\hat{t}_j) < 1. \quad (23)$$

The inequality in (22) holds if it is smaller than the left hand side of (23);

$$\begin{aligned}
\frac{\sum_{j \in \mathcal{K}} f(\hat{t}_j)}{\sum_{l \in \mathcal{K}} F(\hat{t}_l)} [\hat{t}_j - \mathcal{L}(\hat{\mathbf{t}}(\varphi))] &\leq \sum_{j \in \mathcal{K}} \frac{F(\hat{t}_j)}{\sum_{l \in \mathcal{K}} F(\hat{t}_l)} \mathcal{M}'(\hat{t}_j) = \frac{\sum_{j \in \mathcal{K}} f(\hat{t}_j)}{\sum_{l \in \mathcal{K}} F(\hat{t}_l)} [\hat{t}_j - \mathcal{M}^-(\hat{t}_j)] \\
&\Rightarrow \frac{\sum_{j \in \mathcal{K}} f(\hat{t}_j)}{\sum_{l \in \mathcal{K}} F(\hat{t}_l)} \mathcal{M}^-(\hat{t}_j) \leq \frac{\sum_{j \in \mathcal{K}} f(\hat{t}_j)}{\sum_{l \in \mathcal{K}} F(\hat{t}_l)} \mathcal{L}(\hat{\mathbf{t}}(\varphi)) \\
&\Rightarrow \sum_{j \in \mathcal{K}} f(\hat{t}_j) \mathcal{M}^-(\hat{t}_j) \leq \sum_{j \in \mathcal{K}} f(\hat{t}_j) \mathcal{L}(\hat{\mathbf{t}}(\varphi)) = \sum_{j \in \mathcal{K}} f(\hat{t}_j) \sum_{l \in \mathcal{K}} \frac{F(\hat{t}_l)}{\sum_{k \in \mathcal{K}} F(\hat{t}_k)} \mathcal{M}^-(\hat{t}_l) \\
&\Rightarrow \sum_{j \in \mathcal{K}} f(\hat{t}_j) \sum_{l \in \mathcal{K}} F(\hat{t}_l) \mathcal{M}^-(\hat{t}_j) \leq \sum_{l \in \mathcal{K}} f(\hat{t}_l) \sum_{j \in \mathcal{K}} F(\hat{t}_j) \mathcal{M}^-(\hat{t}_j) \\
&\Rightarrow \sum_{j \in \mathcal{K}} f(\hat{t}_j) F(\hat{t}_j) \mathcal{M}^-(\hat{t}_j) + \sum_{j \in \mathcal{K}} \sum_{l \neq j} f(\hat{t}_j) F(\hat{t}_l) \mathcal{M}^-(\hat{t}_j) \leq \sum_{j \in \mathcal{K}} f(\hat{t}_j) F(\hat{t}_j) \mathcal{M}^-(\hat{t}_j) + \sum_{j \in \mathcal{K}} \sum_{l \neq j} f(\hat{t}_l) F(\hat{t}_j) \mathcal{M}^-(\hat{t}_j) \\
&\Rightarrow \sum_{j \in \mathcal{K}} \sum_{l \neq j} f(\hat{t}_j) F(\hat{t}_l) \mathcal{M}^-(\hat{t}_j) \leq \sum_{j \in \mathcal{K}} \sum_{l \neq j} f(\hat{t}_l) F(\hat{t}_j) \mathcal{M}^-(\hat{t}_j) \\
&\Rightarrow 0 \leq \sum_{j \in \mathcal{K}} \sum_{l \neq j} f(\hat{t}_l) F(\hat{t}_j) [\mathcal{M}^-(\hat{t}_j) - \mathcal{M}^-(\hat{t}_l)] \\
&\Rightarrow 0 \leq \sum_{j \in \mathcal{K}} \sum_{l \in \mathcal{K}} f(\hat{t}_l) F(\hat{t}_j) [\mathcal{M}^-(\hat{t}_j) - \mathcal{M}^-(\hat{t}_l)].
\end{aligned}$$

The inequality above holds if for any pair $j < l$

$$f(\hat{t}_l)F(\hat{t}_j)[\mathcal{M}^-(\hat{t}_j) - \mathcal{M}^-(\hat{t}_l)] > f(\hat{t}_j)F(\hat{t}_l)[\mathcal{M}^-(\hat{t}_j) - \mathcal{M}^-(\hat{t}_l)].$$

After rearranging, this inequality becomes

$$\frac{f(\hat{t}_l)}{F(\hat{t}_l)} > \frac{f(\hat{t}_j)}{F(\hat{t}_j)},$$

which holds by log concavity and because $\hat{t}_j > \hat{t}_l$.

E Proof of Lemma 4

An equilibrium obtains where the functions S and D coincide. Applying the implicit function theorem to h , we find that

$$\frac{d\varphi^*}{dx} = -\frac{\partial h/\partial x}{\partial h/\partial \varphi},$$

where, e.g., $\partial h/\partial x = \partial S/\partial x - \partial D/\partial x$. Consider

$$\begin{aligned} K \frac{\partial D}{\partial x} &= \sum_{j \in \mathcal{H}} \frac{\frac{\partial m}{\partial x}(n(\varphi, x) + \Delta(K, j)/\mu) - \frac{\partial n}{\partial x}(m(\varphi, x) + \Delta(K, j)/\mu)}{(n(\varphi, x) + \Delta(K, j)/\mu)^2} \\ &= \sum_{j \in \mathcal{H}} \frac{1}{n(\varphi, x) + \Delta(K, j)/\mu} \left(\frac{\partial m}{\partial x} - \frac{\frac{\partial n}{\partial x}(m(\varphi, x) + \Delta(K, j)/\mu)}{n(\varphi, x) + \Delta(K, j)/\mu} \right) \end{aligned}$$

Using Equation (10), we can replace $1/(n(\varphi, x) + \Delta(K, j)/\mu) = 1/(\mathbb{E}(t) - \mathcal{L}(\varphi, x)) \times 1/r_j$.

Also, note that

$$\frac{m(\varphi, x) + \Delta(K, j)/\mu}{n(\varphi, x) + \Delta(K, j)/\mu} = \frac{1 - r_j}{r_j}.$$

Therefore, the derivative of D is

$$K \frac{\partial D}{\partial x} = \frac{1}{\mathbb{E}(t) - \mathcal{L}(\varphi, x)} \sum_{j \in \mathcal{H}} \left(\frac{\partial m}{\partial x} \frac{1}{r_j} - \frac{\partial n}{\partial x} \frac{1 - r_j}{r_j} \right)$$

To further simplify, consider

$$r_j = \frac{1}{1 + \alpha_j \sum_{l \in \mathcal{K}} F(\hat{t}_l)} \Rightarrow \frac{1}{r_j} = 1 + \alpha_j \sum_{l \in \mathcal{K}} F(\hat{t}_l), \quad \frac{1 - r_j}{r_j} = \alpha_j \sum_{l \in \mathcal{K}} F(\hat{t}_l). \quad (24)$$

Therefore, we can make the following replacement:

$$\begin{aligned} \sum_{j \in \mathcal{H}} \frac{1}{r_j} \frac{1 - r_j}{r_j} &= \sum_{j \in \mathcal{H}} (1 + \alpha_j \sum_{l \in \mathcal{K}} F(\hat{t}_l)) \alpha_j \sum_{l \in \mathcal{K}} F(\hat{t}_l) \\ &= \sum_{l \in \mathcal{K}} F(\hat{t}_l) + \sum_{j \in \mathcal{H}} \alpha_j^2 \left(\sum_{l \in \mathcal{K}} F(\hat{t}_l) \right)^2 \\ &= \sum_{l \in \mathcal{K}} F(\hat{t}_l) (1 + \sum_{j \in \mathcal{H}} \alpha_j^2 \sum_{l \in \mathcal{K}} F(\hat{t}_l)). \end{aligned}$$

Defining $\tilde{r} \equiv \frac{1}{1 + \sum_{j \in \mathcal{H}} \alpha_j^2 \sum_{l \in \mathcal{K}} F(\hat{t}_l)}$, the derivative of h with respect to x becomes

$$\frac{\partial h}{\partial x} = \frac{1}{\mathbb{E}(t) - \mathcal{L}(\varphi, x)} \left[\sum_{j \in \mathcal{K}} f(\hat{t}_j(\varphi, x)) \frac{\partial \hat{t}_j}{\partial x} (\mathbb{E}(t) - \mathcal{L}(\varphi, x)) - \left(\frac{\partial m}{\partial x} \sum_{j \in \mathcal{H}} \frac{1}{r_j} - \frac{\partial n}{\partial x} \sum_{j \in \mathcal{K}} \frac{F(\hat{t}_j)}{\tilde{r}} \right) \right].$$

Multiplying and dividing the r.h.s by $\tilde{r}^2 \sum_{j \in \mathcal{K}} \alpha_j^2$;

$$\begin{aligned} \frac{\partial h}{\partial x} &= \frac{1}{\underbrace{\sum_{j \in \mathcal{K}} \alpha_j^2 (K - k^*) \tilde{r}^2 (\mathbb{E}(t) - \mathcal{L}(\varphi, x))}_{\equiv \beta}} \times \\ &\times \left[\underbrace{\tilde{r}^2 \sum_{j \in \mathcal{K}} \alpha_j^2 \sum_{j \in \mathcal{K}} f(\hat{t}_j(\varphi, x)) \frac{\partial \hat{t}_j}{\partial x} (\mathbb{E}(t) - \mathcal{L}(\varphi, x))}_{= -\frac{\partial \tilde{r}}{\partial x}} - \left(\frac{\partial m}{\partial x} \tilde{r}^2 \sum_{j \in \mathcal{K}} \alpha_j^2 \sum_{j \in \mathcal{H}} \frac{1}{r_j} - \frac{\partial n}{\partial x} \tilde{r} \underbrace{\sum_{j \in \mathcal{K}} \alpha_j^2 \sum_{j \in \mathcal{K}} F(\hat{t}_j)}_{= 1 - \tilde{r}} \right) \right]. \end{aligned}$$

Plugging in (24), the middle term becomes

$$\begin{aligned} \frac{\partial m}{\partial x} \tilde{r}^2 \sum_{j \in \mathcal{K}} \alpha_j^2 \sum_{j \in \mathcal{H}} \frac{1}{r_j} &= \frac{\partial m}{\partial x} \tilde{r}^2 \sum_{j \in \mathcal{K}} \alpha_j^2 (K - k^* + \sum_{j \in \mathcal{K}} F(\hat{t}_j)) \\ &= \frac{\partial m}{\partial x} \tilde{r} \underbrace{\left(\tilde{r} \sum_{j \in \mathcal{K}} \alpha_j^2 (K - k^*) + (1 - \tilde{r}) \right)}_{\equiv \xi}. \end{aligned}$$

We arrive at

$$\frac{\partial h}{\partial x} = -\beta \left[\frac{\partial \tilde{r}}{\partial x} (\mathbb{E}(t) - \mathcal{L}(\varphi, x)) + \left(\tilde{r} \xi \frac{\partial m}{\partial x} - (1 - \tilde{r}) \frac{\partial n}{\partial x} \right) \right].$$

Therefore,

$$\frac{d\varphi^*}{dx} = \frac{\beta \left[\frac{\partial \tilde{r}}{\partial x} (\mathbb{E}(t) - \mathcal{L}(\varphi, x)) + \left(\tilde{r} \xi \frac{\partial m}{\partial x} - (1 - \tilde{r}) \frac{\partial n}{\partial x} \right) \right]}{\partial h / \partial \varphi}.$$

From the proof of Proposition 2 we know that the denominator in the equation above is positive, which implies that, for $\frac{d\varphi^*}{dx}$ to be positive, the numerator must be positive.

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